High-Precision Measurement of $G_M^n$ With CLAS

Jerry Gilfoyle for the E5 group
Physics Department, University of Richmond, Virginia

Outline:
1. Motivation.
2. Previous Measurements.
3. Necessary Background.
4. The Ratio Method.
5. Results.
6. Conclusions.
Scientific Motivation

• To explore the ground state structure of the proton and neutron.

• $G^m_M(Q^2)$ is a fundamental observable related to the spatial distribution of the magnetization in the neutron.

• Elastic form factors ($G^m_M$, $G^n_E$, $G^p_M$, and $G^n_E$) provide key constraints on generalized parton distributions (GPDs) which promise to give us a three-dimensional picture of hadrons.

• Elastic hadronic form factors are a fundamental challenge for lattice QCD.

• Required for extracting the strange quark distributions in the proton.

• Part of a broad effort to understand how nucleons are ‘constructed from the quarks and gluons of QCD’. *

Current Status of Neutron Elastic Form Factors

- $G^n_M$ and $G^n_E$.

Some Necessary Background

- It is convenient to express the cross section in terms of the Sachs form factors.

\[
\frac{d\sigma}{d\Omega} = \sigma_{Mott} \left( G^2_E + \frac{\tau}{\epsilon} G^2_M \right) \left( \frac{1}{1 + \tau} \right)
\]

where

\[
\tau = \frac{Q^2}{4M^2}, \quad \epsilon = \frac{1}{1 + 2(1 + \tau) \tan^2(\frac{\theta}{2})}, \quad \sigma_{Mott} = \frac{\alpha^2 E' \cos^2(\frac{\theta}{2})}{4E^3 \sin^4(\frac{\theta}{2})}.
\]

- We can now take the ratio of the \(e-\)p and \(e-\)n cross sections (the ratio method).

\[
R = \frac{\frac{d\sigma}{d\Omega}(D(e, e'n))}{\frac{d\sigma}{d\Omega}(D(e, e'p))} = a(Q^2) \frac{G^2_E + \tau G^2_M}{1 + \tau} + \frac{2\tau G^2_M}{G^2_E + \tau G^2_M} \frac{G^2_E + \tau G^2_M}{1 + \tau} + 2\tau G^2_M \tan^2(\frac{\theta}{2})
\]
Some More Necessary Background

- To select quasielastic events (more later) we will use a cut on $\theta_{pq}$ shown here.
Experimental Details

- JLab and CLAS.

- Data Set: 2.3 billion triggers at three sets of running conditions. Two sets at beam energies $4.2 \text{ GeV}$ and $2.6 \text{ GeV}$ with positive torus polarity (electrons inbending). Another data set was collected at $2.6 \text{ GeV}$ with reversed torus polarity (electrons outbending) to reach lower $Q^2$. 
More Experimental Details

• Dual target cell with liquid hydrogen and deuterium. The hydrogen cell was downstream and separated from the deuterium target by 4.7-cm gap. Enables us to perform \textit{in situ} calibrations during data collection.

• Targets are well separated in tracking.
The Ratio Method - Event Selection

- Use $e - n/e - p$ ratio to reduce systematic uncertainties.


- $e - n$ selection: same criteria for electrons; use TOF and calorimeter as independent measurements of the neutron with cuts to reject photons.

- Quasi-elastic event selection: Apply a maximum $\theta_{pq}$ cut to eliminate inelastic events plus a cut on $W^2$.

- Acceptance matching: Use the quasi-elastic electron kinematics to predict if the nucleon (proton or neutron) lies in CLAS acceptance. Require both hypotheses to be satisfied.

- Neutrons and protons treated exactly the same whenever possible.
The Ratio Method - Corrections

Neutron detection efficiency:

1. Use the $ep \rightarrow e' \pi^+ n$ reaction from the hydrogen target as a source of tagged neutrons in the TOF and calorimeter.

2. Standard CLAS cuts for electron selection.

3. For $\pi^+$, use positive tracks, cut on the difference between $\beta$ measured from tracking and from time-of-flight.

4. For neutrons, $ep \rightarrow e\pi^+ X$ for $0.9 < m_X < 0.95 \text{ GeV}/c^2$.

5. In the calorimeter use the neutron momentum $\vec{p}_n$ to determine the location of a hit in the fiducial region (reconstructed event) and search for that neutron (a found event if it’s there).
6. In the TOF use the neutron momentum $\vec{p}_n$ to predict which TOF paddle is hit (reconstructed event) and then search in that paddle (a found event if it’s there). Reduce photon background by requiring a minimum energy deposited.

7. We have made two measurements of the neutron detection efficiency (calorimeter and TOF) for each set of running conditions.
The Ratio Method - Corrections

Proton detection efficiency:

1. Use $ep \rightarrow e'p$ elastic scattering from hydrogen target as a source of tagged protons.

2. Standard CLAS cuts for electron selection with a $W^2$ cut to select $ep$ elastic events.

3. Protons were identified as positive tracks with a coplanarity cut applied.

4. In the TOF use the missing momentum from $ep \rightarrow e'X$ to predict the TOF paddle that will be struck by the proton (a reconstructed event). Search that paddle or an adjacent one for a positively-charged particle (a found event if it’s there). Results below are for sector 1 in CLAS.

![Efficiency vs Paddle Number Graph](image-url)
The Ratio Method - Corrections

- Nuclear effects: The $e^{-}n/e^{-}p$ ratio for free nucleons can be altered here because we measure the quasielastic scattering from bound nucleons. This factor $a(Q^2)$ was calculated and we compared results from Jeschonnek and Arenhoevel. Where the calculations overlap in $Q^2$, the average correction to $R$ is 0.994 and we assigned a systematic uncertainty of 0.6%.

- Radiative corrections: Calculated for exclusive $D(e, e'p)n$ with the code EXCLURAD by Afanasev and Gilfoyle (CLAS-Note 2005-022). The ratio of the correction factors for $e^{-}n/e^{-}p$ events is close to unity.

![Graph](image.png)
## The Ratio Method - Systematic Errors

<table>
<thead>
<tr>
<th>Quantity</th>
<th>2.6 GeV</th>
<th>4.2 GeV</th>
<th>Quantity</th>
<th>2.6 GeV</th>
<th>4.2 GeV</th>
</tr>
</thead>
<tbody>
<tr>
<td>Calorimeter neutron efficiency parameterization</td>
<td>&lt; 1.5</td>
<td>&lt; 1.0</td>
<td>TOF neutron efficiency parameterization</td>
<td>&lt; 2.0</td>
<td>&lt; 2.0</td>
</tr>
<tr>
<td>proton $\sigma$</td>
<td>&lt; 1.0</td>
<td>&lt; 1.5</td>
<td>$G_E^n$</td>
<td>&lt; 0.5</td>
<td>&lt; 0.7</td>
</tr>
<tr>
<td>neutron accidentals</td>
<td>&lt; 0.07</td>
<td>&lt; 0.3</td>
<td>neutron MM cut</td>
<td>&lt; 0.5</td>
<td>&lt; 0.07</td>
</tr>
<tr>
<td>neutron proximity cut</td>
<td>&lt; 0.22</td>
<td>&lt; 0.15</td>
<td>proton efficiency</td>
<td>&lt; 0.3</td>
<td>&lt; 0.35</td>
</tr>
<tr>
<td>Fermi loss correction</td>
<td>&lt; 0.8</td>
<td>&lt; 0.9</td>
<td>$\theta_{pq}$ cut</td>
<td>&lt; 0.4</td>
<td>&lt; 1.0</td>
</tr>
<tr>
<td>Nuclear Corrections</td>
<td>&lt; 0.17</td>
<td>&lt; 0.2</td>
<td>Radiative corrections</td>
<td>&lt; 0.05</td>
<td>&lt; 0.06</td>
</tr>
</tbody>
</table>

Upper limits on estimated systematic error for different contributions.
Results - Overlaps and Final Averages

- Overlapping measurements of $G^n_M$ scaled by the dipole are consistent.

- Weighted-average $G^n_M/\mu_n G_D$ and systematic uncertainty $\frac{\delta G^n_M}{G^n_M} \times 100 (< 2.5\%)$. 

Workshop on Exclusive Reactions at High Momentum Transfer, May 21-24, 2007
Results - Comparison with Existing Data

\[ G_M^p(\mu n G_D) \]

Combined Systematic Uncertainty

Workshop on Exclusive Reactions at High Momentum Transfer, May 21-24, 2007
Conclusions

- We have measured the neutron magnetic form factor $G^m_M$ over the range $Q^2 = 0.5 - 4.5 \ (\text{GeV}/c)^2$ to a precision better than 2.5%.

- The four different measurements of $G^m_M$ at two beam energies with the calorimeter and the TOF system in CLAS are consistent.

- Some differences exist with previous measurements at $Q^2 < 1 \ (\text{GeV}/c)^2$.

- The results are consistent with the dipole approximation within 5% across almost the full range of $Q^2$. 
Current Status and the Future

- Analysis of the normal-torus-field data at 2.6 GeV and 4.2 GeV are under CLAS Collaboration review.
- The reversed-torus-polarity data set is still being worked on.
- We submitted a Letter-of-Intent to measure $G_n^M$ at 12 GeV to the JLab PAC in June, 2006 and were ‘encouraged’ to submit a full proposal.
- We are preparing that proposal now. The expected quality of the data is shown here.
Published Measurements of Elastic Form Factors

- $G^n_M$
- $G^p_M$
- $G^p_E/G^p_M$

The Ratio Method - Systematic Errors

- Calorimeter neutron detection efficiency parameterization: The neutron efficiency was fitted with a third order polynomial plus a flat region at higher momentum. To study systematic uncertainties the highest order term was dropped and the ratio $R$ regenerated. The upper limit on the range of differences for the different extractions of $R$ was assigned the systematic uncertainty.

- TOF neutron detection efficiency parameterization: Similar to calorimeter extraction except the second and third order terms in the polynomial were dropped.

<table>
<thead>
<tr>
<th>Detector</th>
<th>2.6 GeV</th>
<th>4.2 GeV</th>
</tr>
</thead>
<tbody>
<tr>
<td>Calorimeter</td>
<td>1.5</td>
<td>1.0</td>
</tr>
<tr>
<td>TOF</td>
<td>2.0</td>
<td>2.0</td>
</tr>
</tbody>
</table>

Percentage systematic uncertainties in neutron efficiency parameterization.

- These are the largest contributions from this measurement.
The Ratio Method - Corrections

- Fermi motion: The efficiency measurements rely on the quasielastic electron kinematics to predict whether or not the nucleon reaches the fiducial region of the TOF or the calorimeter. Fermi motion in the target can cause nucleons to migrate out of the CLAS acceptance. This effect was calculated in simulation and a sample of the results is shown here.