What is a postulate?

 suggest or assume the existence, fact, or truth of (something) as a basis for reasoning, discussion, or belief.

"a theory postulated by a respected scientist" synonyms: suggest, advance, posit, hypothesize, propose, assume

(in ecclesiastical law) nominate or elect (someone) to an ecclesiastical office subject to the sanction of a higher authority.

How do you know it's correct? DATA!

See here for an example of impeccable logic.

- **()** Each physical, measurable quantity, A, has a corresponding operator, \hat{A} , that satisfies the eigenvalue equation $\hat{A} \phi = a\phi$ and measuring that quantity yields the eigenvalues of \hat{A} .
- **②** Measurement of the observable A leaves the system in a state that is an eigenfunction of \hat{A} .
- **3** The state of a system is represented by a wave function Ψ that is continuous, differentiable and contains all possible information about the system. The 'intensity' is proportional to $|\Psi|^2$ and is interpreted as a probability. The average value of any observable A is $\langle A \rangle = \int_{all \ space} \Psi^* \hat{A} \ \Psi d\vec{r}$.
- The time and spatial dependence of Ψ(x, t) is determined by the time dependent Schroedinger equation.

$$i\hbar \frac{\partial}{\partial t}\Psi(x,t) = -\frac{\hbar^2}{2\mu}\frac{\partial^2}{\partial x^2}\Psi(x,t) + V(x)\Psi(x,t) \qquad \mu \equiv ext{ reduced mass.}$$

Consider the infinite rectangular well potential shown in the figure below.

- What is the time-independent Schroedinger equation for this potential?
- What is the general solution to the previous question?
- What are the boundary conditions the solution must satisfy?
- What is the particular solution for this potential?
- What is the energy of the particular solution?



The Infinite Rectangular Well Potential - Energy Levels 4



Some Math

5

The solutions of the Schroedinger equation form a Hilbert space.

1 They are linear, *i.e.* superposition/interference is built in.

- If a is a constant and $\phi(x)$ is an element of the space, then so is $a\phi(x)$.
- If $\phi_1(x)$ and $\phi_2(x)$ are elements, then so is $\phi_1(x) + \phi_2(x)$.

An inner product is defined and all elements have a norm.

$$\langle \phi_n | \psi
angle = \int_{-\infty}^{\infty} \phi_n^* \psi \, dx$$
 and $\langle \phi_n | \phi_n
angle = \int_{-\infty}^{\infty} \phi_n^* \phi_n dx = 1$

The solutions are complete.

$$|\psi\rangle = \sum_{n=0}^{\infty} b_n |\phi_n\rangle$$

③ The solutions are orthonormal so $\langle \phi_n | \phi_{n'} \rangle = \delta_{n,n'}$.

The operators are Hermitian - their eigenvalues are real.

Jerry Gilfoyle

Consider the infinite rectangular well potential shown in the figure below with an initial wave packet defined in the following way.

$$\begin{array}{rcl} \Psi(x,0) & = & \frac{1}{\sqrt{d}} & x_0 < x < x_1 & \text{and} & d = x_1 - x_0 \\ & = & 0 & \text{otherwise} \end{array}$$

- What possible values are obtained in an energy measurement?
- What eigenfunctions contribute to this wave packet and what are their probabilities?
- What will many measurements of the energy give?



Apply the Rules More: A Particle in a Box

Consider the infinite rectangular well potential shown in the figure below with an initial wave packet defined in the following way.

$$\begin{array}{rcl} \Psi(x,0) & = & \frac{1}{\sqrt{d}} & x_0 < x < x_1 & \text{and} & d = x_1 - x_0 \\ & = & 0 & \text{otherwise} \end{array}$$

- What possible values are obtained in an energy measurement?
- What eigenfunctions contribute to this wave packet and what are their probabilities?
- What will many measurements of the energy give?



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$$\lim_{x \to c} f(x) = \lim_{x \to c} g(x) = 0 \quad \text{or} \quad \lim_{x \to c} f(x) = \lim_{x \to c} g(x) = \pm \infty$$

and
$$\lim_{x \to c} \frac{f'(x)}{g'(x)}$$

exists, then

$$\lim_{x \to c} \frac{f(x)}{g(x)} = \lim_{x \to c} \frac{f'(x)}{g'(x)}$$

















Probabilities of Different Final States



Probabilities of Different Final States - 2



Probabilities of Different Final States - 3



Probabilities of Different Final States - 4



Why a page limit?

Possible Existence of a Neutron

It has been shown by Bothe and others that beryllium when bombarded by s-particles of polonium buy main an adjustion of great penetrating power, which has an absorption coefficient in lead of about 0.3 (cm.)⁻¹. Recently Mme. Curie-Joliot and M. Joliot found, when measuring the ionisation produced by this beryllium radiation in a vessel with a thin window, that the ionisation increased when matter containing hydrogen was placed in front of the window. The effect appeared to be due to the ejection of protons with velocities up to a maximum of nearly 3 × 10⁹ cm. per sec. They suggested that the transference of energy to the proton was by a process similar to the Compton effect, and estimated that the beryllium radiation had a quantum energy of 50 × 10⁴ electron volts. I have made some experiments using the valve counter to examine the properties of this radiation excited in beryllium. The valve counter consists of a small ionisation chamber connected to an amplifier. and the sudden production of ions by the entry of a particle, such as a proton or a-particle, is recorded by the deflexion of an oscillograph. These experiments have shown that the radiation ejects particles from hydrogen, helium, lithium, beryllium, carbon, air, and argon. The particles ejected from hydrogen behave, as regards range and ionising power, like protons with speeds up to about 3.2 × 10° cm. per sec. The particles from the other elements have a large ionising power, and appear to be in each case recoil atoms of the elements.

If we see that the ejection of the proton to a Compton recoil from a quantum of 32×10^{-6} sector volts, then the nitrogen recoil atom arising by a similar process should have an energy nod greater than about 10,000 kms, and have a runge in air at NTLP. of about 1.3 mm. Actually, some of the recoil atoms in nitrogen produce at least 30,000 ions. In collaboration with Dr. Feather 1 have observed the rungs, estimated visually vans sometimes as much as 3 mm. at NT-P.

Thus results, and other 1 have obtained in the come of the type, and way, diffusible to explain an end of the second second second second second second is a quantum radiation, if energy and momentum sequences in the second second second second second sequences in the second framework and the second se

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Width of a distribution?



The Quantum Program in One Dimension - So Far 21

Solve the Schroedinger equation to get eigenfunctions and eigenvalues.

$$-\frac{\hbar^2}{2m}\frac{\partial^2\phi(x)}{\partial x^2}+V\phi(x)=E_n\phi(x)$$

2 For an initial wave packet $\psi(x)$ use the completeness of the eigenfunctions.

$$|\psi(x)
angle = \sum_{n=1}^{\infty} b_n |\phi(x)
angle$$

③ Apply the orthonormality $\langle \phi_m | \phi_n \rangle = \delta_{m,n}$.

$$\langle \phi_m | \psi \rangle = \langle \phi_m | \left(\sum_{n=1}^{\infty} b_n | \phi \rangle \right) = b_m = \int_{-\infty}^{\infty} \phi_m^* \left(\sum_{n=1}^{\infty} b_n | \phi \rangle \right) dx$$

• Get the probability P_n for measuring E_n from $|\psi\rangle$.

$$P_n = |b_n|^2$$

- Do the free particle solution.
- Out in the time evolution.

Consider a case of one dimensional nuclear 'fusion'. A neutron is in the potential well of a nucleus that we will approximate with an infinite square well with walls at x = 0 and x = a. The eigenfunctions and eigenvalues are

$$E_n = \frac{n^2 \hbar^2 \pi^2}{2ma^2} \qquad \phi_n = \sqrt{\frac{2}{a}} \sin\left(\frac{n\pi x}{a}\right) \qquad 0 \le x \le a$$
$$= 0 \qquad \qquad x < 0 \text{ and } x > a$$

The neutron is in the n = 4 state when it fuses with another nucleus that is the same size, instantly putting the neutron in a new infinite square well with walls at x = 0 and x = 2a.

- What are the new eigenfunctions and eigenvalues of the fused system?
- What is the spectral distribution?
- What is the average energy? Use the b_n 's.

Spectral Distribution for One-Dimensional Nuclear Fusion 23



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The Rules of the Quantum Game

Spectral Distribution for One-Dimensional Nuclear Fusion 24



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The Rules of the Quantum Game

Spectral Distribution for One-Dimensional Nuclear Fusion 25



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The Rules of the Quantum Game