

2.23

$$p = \frac{h}{\lambda}$$

$$E = \frac{p^2}{2m}$$

$$\lambda = \frac{h}{p} \quad p = \sqrt{2mE}$$

$$= \frac{h}{\sqrt{2mE}}$$

$$h = 6.626 \times 10^{-34} \text{ J}\cdot\text{s}$$

$$m = m_e = 9.1 \times 10^{-31} \text{ kg}$$

$$E \text{ in eV}$$

$$a. \quad \lambda_e = \frac{h}{\sqrt{2m_e}} \frac{1}{E^{1/2}}$$

$$= \frac{6.626 \times 10^{-34} \text{ J}\cdot\text{s}}{\sqrt{2} (9.1 \times 10^{-31} \text{ kg})^{1/2}} \frac{1}{E^{1/2}}$$

$$= \left( 4.912 \times 10^{-19} \frac{\text{J}\cdot\text{s}}{\text{kg}^{1/2}} \right) \left( \frac{1}{E \times 1.6 \times 10^{-19} \text{ J/eV}} \right)^{1/2}$$

$$= 1.228 \times 10^{-9} \frac{\text{J}\cdot\text{s}}{\text{kg}^{1/2} \text{ J}^{1/2}} \frac{1}{E^{1/2}} \sqrt{\text{eV}}$$

$$\frac{\text{J}\cdot\text{s}}{\text{kg}^{1/2} \text{ J}^{1/2}} = \frac{\text{kg} \frac{\text{m}^2}{\text{s}^2} \cdot \text{s}}{\text{kg}^{1/2} \left( \text{kg} \frac{\text{m}^2}{\text{s}^2} \right)^{1/2}} = \frac{\text{kg} \frac{\text{m}^2}{\text{s}}}{\text{kg}^{1/2} \cdot \text{kg}^{1/2} \frac{\text{m}}{\text{s}}} = \frac{\text{kg} \frac{\text{m}^2}{\text{s}}}{\text{kg} \frac{\text{m}}{\text{s}}} = \text{m}$$

$$= 1.228 \times 10^{-9} \text{ m} \frac{1}{E^{1/2}} \times \frac{100 \text{ cm}}{\text{m}}$$

→ has to be in eV  
to cancel  $\sqrt{\text{eV}}$ .

$$\lambda_e = \frac{12.3 \times 10^{-8} \text{ cm}}{E^{1/2}}$$

$$b. \lambda_p = \frac{h}{\sqrt{2m_p E}}$$

$$m = m_p = 1.67 \times 10^{-27} \text{ kg}$$

$$= \frac{6.626 \times 10^{-34} \text{ J-s}}{\sqrt{2} (1.67 \times 10^{-27} \text{ kg})^{1/2}} \frac{1}{E^{1/2}}$$

$$= \left( 1.147 \times 10^{-20} \frac{\text{J-s}}{\text{kg}^{1/2}} \right) \left( \frac{1}{E \times 1.6 \times 10^{-19} \text{ J/eV}} \right)^{1/2}$$

$$= 2.866 \times 10^{-11} \frac{\text{J-s}}{\text{kg}^{1/2} \cdot \text{J}^{1/2}} \frac{1}{E^{1/2}} \sqrt{\text{eV}}$$

= m as before

$$= 2.866 \times 10^{-11} \text{ m} \times \frac{100 \text{ am}}{\text{m}} \frac{1}{E^{1/2}}$$

$$= \frac{0.29 \times 10^{-8} \text{ am}}{E^{1/2}}$$

↳ has to be in eV to cancel  $\sqrt{\text{eV}}$