

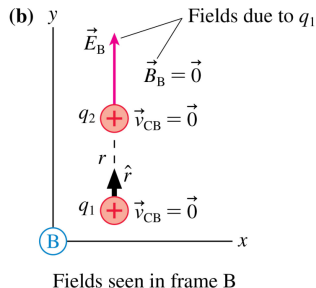
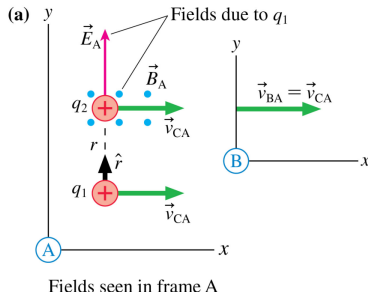
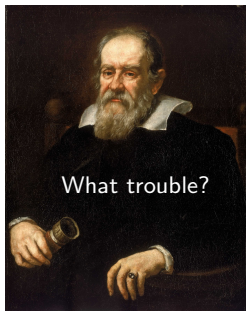
Filling out the Card

- ① List which physics and math courses you have had especially Math Methods, Quantum Mechanics, Classical Mechanics, Statistical Mechanics, Electricity and Magnetism.
- ② Do you have experience with *Mathematica*?
- ③ What are your pronouns?

The Trouble With Galileo - 1

2

Consider Figure a. Two positive charges are moving side-by-side in frame A (also called the Home frame) with velocity $\vec{v}_{BA} = \vec{v}_{CA}$. What are the fields $\vec{E}_A$ and $\vec{B}_A$ of charge q_1 at the position of charge q_2 in frame A ? In Figure b the B/Other frame is moving with the same velocity as the two charges. What are $\vec{E}_B$ and $\vec{B}_B$ at the position of q_2 ?



Physics is the same in all inertial reference frames (hopefully).

Galilean
$x' = x - vt$
$y' = y$
$z' = z$
$t' = t$
$v'_x = v_x - v_O$
$v'_y = v_y$
$v'_z = v_z$

primes refer to the frame moving with velocity v_O .

v_O - velocity of moving/Other/B frame.

v_i - i^{th} component of the velocity in the stationary/Home/A frame.

v'_i - i^{th} component of the velocity in the moving/Other/B frame.

Galilean

$x' \equiv x - vt$

Are Newton's Laws consistent with the Galilean transformations?

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Galilean

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Are Newton's Laws consistent with the Galilean transformations?

Yes! The laws of physics are the same in all inertial frames.

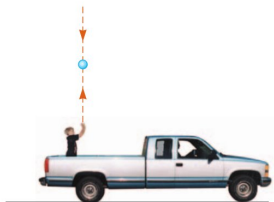
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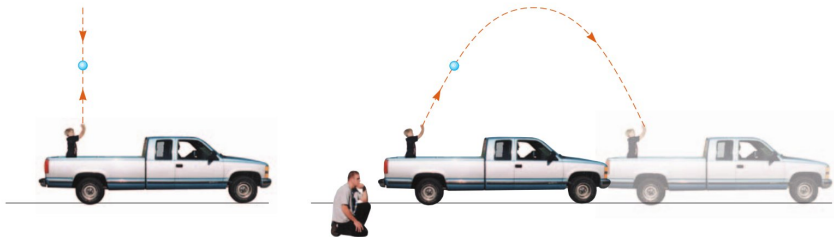
v_i - i^{th} component of the velocity in the stationary/Home/A frame.

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What changes in the trajectory of a tossed ball between the Home frame and the Other frame?



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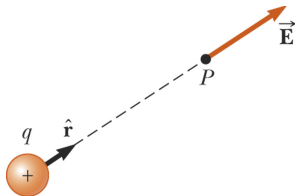
Coulomb's Law

$$d\vec{E} = k_e \frac{dq\hat{r}}{r^2} = \frac{1}{4\pi\epsilon_0} \frac{dq\hat{r}}{r^2}$$

Apply GT to Electric and Magnetic Fields - 1 10

Coulomb's Law

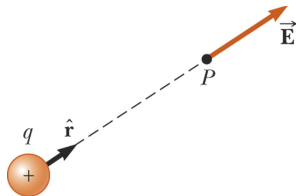
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Apply GT to Electric and Magnetic Fields - 1 11

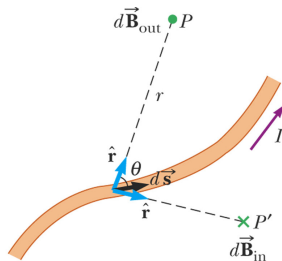
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Biot-Savart Law

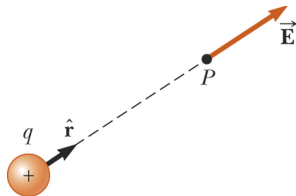
$$d\vec{B} = k_m \frac{I d\vec{s} \times \hat{r}}{r^2} = \frac{\mu_0}{4\pi} \frac{I d\vec{s} \times \hat{r}}{r^2}$$



Apply GT to Electric and Magnetic Fields - 1 12

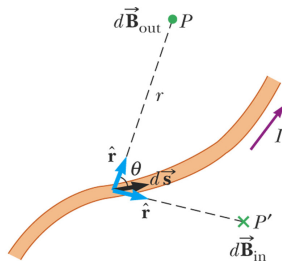
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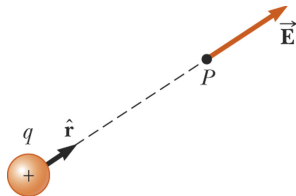
$$\begin{aligned} d\vec{B} &= k_m \frac{I d\vec{s} \times \hat{r}}{r^2} = \frac{\mu_0}{4\pi} \frac{I d\vec{s} \times \hat{r}}{r^2} \\ &= k_m \frac{q \vec{v} \times \hat{r}}{r^2} = \frac{\mu_0}{4\pi} \frac{dq \vec{v} \times \hat{r}}{r^2} \end{aligned}$$



Apply GT to Electric and Magnetic Fields - 1 13

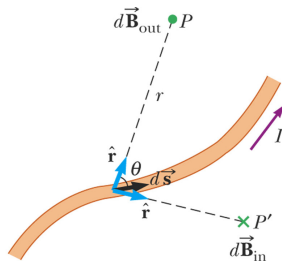
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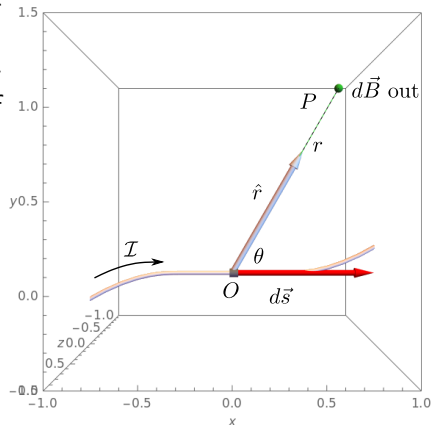
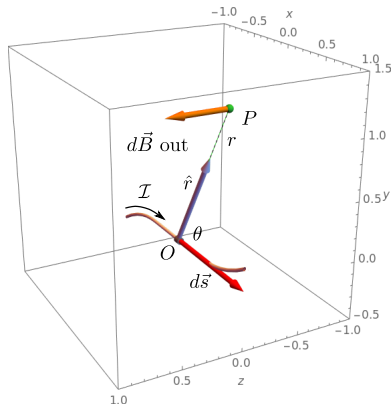
$$\begin{aligned} d\vec{B} &= k_m \frac{Id\vec{s} \times \hat{r}}{r^2} = \frac{\mu_0}{4\pi} \frac{Id\vec{s} \times \hat{r}}{r^2} \\ &= k_m \frac{q\vec{v} \times \hat{r}}{r^2} = \frac{\mu_0}{4\pi} \frac{dq \vec{v} \times \hat{r}}{r^2} \end{aligned}$$



Electromagnetic Force Law

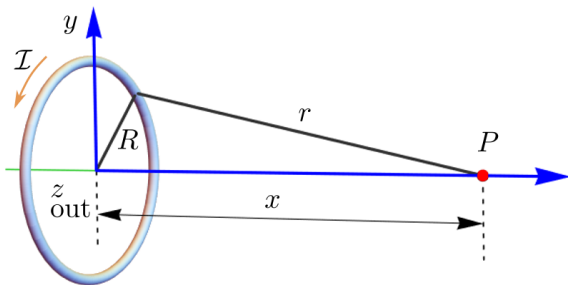
$$\vec{F} = q \left(\vec{E} + \vec{v} \times \vec{B} \right)$$

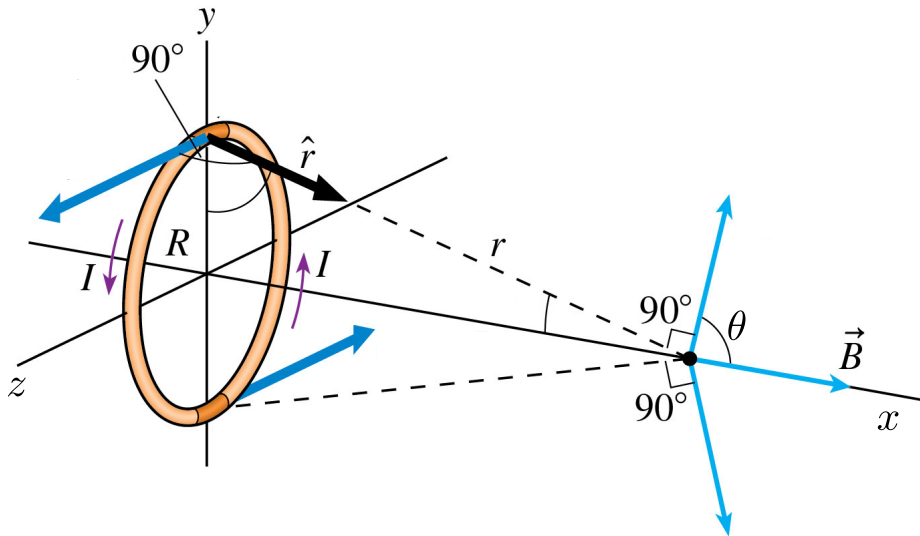
The figures show two views of a segment of a current. What is the magnetic field $d\vec{B}$ at the point P due to the infinitesimal chunk of current at O in terms of the current $\mathcal{I}$, $d\vec{s}$, $\vec{r}$, and the angle θ ?



The current $\mathcal{I}$, $\vec{r}$, and $d\vec{s}$ all lie in the same plane.

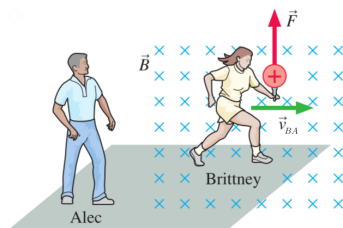
(1) A ring of radius R as shown in the figure below has a current $\mathcal{I}$. Calculate the magnetic field $\vec{B}$ along the axis of the ring at a point lying a distance x from the center of the ring. Get your answer in terms of R , x , $\mathcal{I}$. (2) In Neils Bohr's 1913 model of the hydrogen atom an electron circles the proton at a distance $R = 5.29 \times 10^{-11} \text{ m}$ with a speed $v = 2.19 \times 10^6 \text{ m/s}$. What is the magnetic field at the position of the proton created by the electron's orbit?



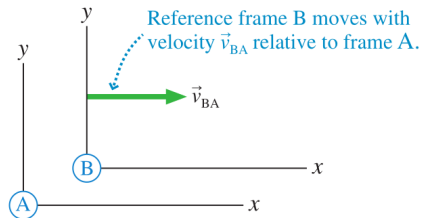


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- ① primes - in frame with velocity v_O .
- ② v_O - velocity of moving/Other/B frame.
- ③ v_i - velocity component in stationary/Home/A frame.
- ④ v'_i - velocity component in moving/Other/B frame.



Charge q moves through a magnetic field established by Alec.



$$\begin{aligned}\vec{E}_B &= \vec{E}_A + \vec{v}_{BA} \times \vec{B}_A \\ \vec{B}_B &= \vec{B}_A - \mu_0\epsilon_0\vec{v}_{BA} \times \vec{E}_A \\ \mu_0\epsilon_0 &= \frac{1}{c^2}\end{aligned}$$

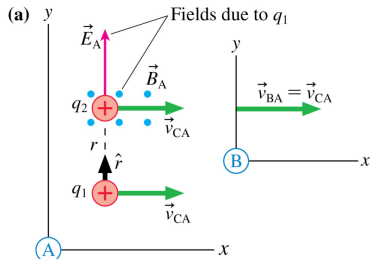
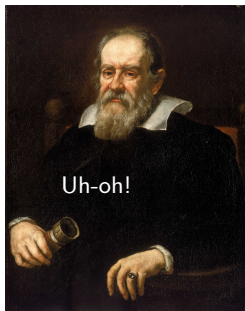
The vector $\vec{v}_{BA}$ is the velocity of the Other frame.

* *Classical electromagnetism and special relativity*, https://en.wikipedia.org/wiki/Classical_electromagnetism_and_special_relativity

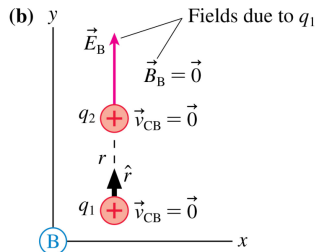
The Trouble With Galileo - 2

19

Consider Figure a. Two positive charges move side-by-side through frame A (the Home frame) with velocity $\vec{v}_{BA} = \vec{v}_{CA}$. What are the fields $\vec{E}_A$ and $\vec{B}_A$ of charge q_1 at the position of charge q_2 in frame A ? In Figure b the B/Other frame moves with the same velocity as the two charges. What are $\vec{E}_B$ and $\vec{B}_B$ at the position of q_2 ?

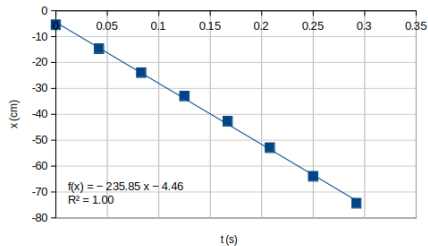


Fields seen in frame A

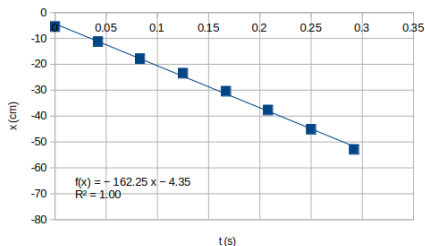


Fields seen in frame B

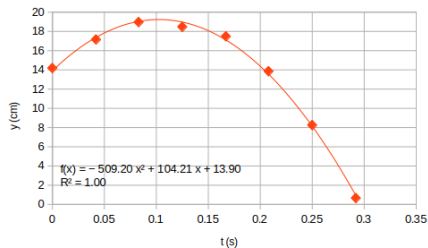
Fixed Origin



Moving Origin



Fixed Origin



Moving Origin

