- Name:
- Did you take Phys 131 and who was your instructor?
- How many semesters of physics before this course (high school or college)?
- How many semesters of calculus before this course (high school or college)?
- Preferred personal pronouns?


## What are you made of and how do you know? 2

## What are you made of and how do you know? 3

## Dalton's Atomic Theory (1808)

(1) All matter consists of tiny particles.
(2) Atoms are indestructible and unchangeable.
(3) Elements are characterized by the mass of their atoms.
(4) When elements react, their atoms combine in simple, whole-number ratios.

from A New System of Chemical Philosophy (1808) by John Dalton

## What are you made of and how do you know?

## Dalton's Atomic Theory (1808)

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(4) When elements react, their atoms combine in simple, whole-number ratios.

Boltzmann's Kinetic Theory (1905)
(1) Matter consists of tiny particles.
(2) Use Newtonian physics to calculate ideal gas properties like the heat capacity/specific heat.
(3) Connects bulk properties to microscopic motion of atoms.

from A New System of Chemical Philosophy (1808) by John Dalton


## Specific Heats of Ideal Gases

Assume that a pure, ideal gas is made of tiny particles that bounce into each other and the walls of their cubic container of side $\ell$. Show the average pressure $P$ exerted by this gas is

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P=\frac{1}{3} \frac{N}{V} m \overline{v_{\text {total }}^{2}}
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$$

Is this right?
$N$ - number of particles $\quad V=\ell^{3}$
$k_{B}$ - Boltzmann constant $m$ - atomic mass
$N_{A}$ - Avogadro's number $\quad v_{\text {total }}$ - atom's speed


## The Plan



## Temperature and Heat



## Temperature and Heat



## Temperature and Heat

Heat $(Q)$ is thermal energy transferred from one place or body to another due to a difference in temperature. Thermal energy is the mechanical energy (kinetic and potential) associated with atomic motion in an object.


## Temperature and Heat

## 10

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## Calorimetry/Energy Conservation

Two ice cubes each with mass $m_{I}=0.050 \mathrm{~kg}$ are taken from a freezer at $T_{0}=0^{\circ} \mathrm{C}$ and dropped into a container holding $m_{w}=1.0 \mathrm{~kg}$ of water at $T_{1}=25^{\circ} \mathrm{C}$. What will be the final temperature of the liquid? Assume the container absorbs no heat.


$$
\begin{aligned}
& c_{\text {ice }}=2090 \mathrm{~J} / \mathrm{kg}-K \\
& c_{w}=4186 \mathrm{~J} / \mathrm{kg}-K \\
& L_{f}=3.33 \times 10^{5} \mathrm{~J} / \mathrm{kg}
\end{aligned}
$$

## Calorimetry/Energy Conservation 12

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\end{aligned}
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## The Plan



## Heat of Vaporization of Liquid Nitrogen Lab 14




## The First Law of Thermodynamics

Let 1.00 kg of liquid water at $100^{\circ} \mathrm{C}$ be converted to steam at $100^{\circ} \mathrm{C}$. The water is contained in a cylinder with a movable piston of negligible mass that sits right on top of the water at the start. The volume changes from an initial value of $1.00 \times 10^{-3} \mathrm{~m}^{3}$ as a liquid to $1.671 \mathrm{~m}^{3}$ as steam. The latent heat of vaporization of water is $L_{V}=2.26 \times 10^{6} \mathrm{~J} / \mathrm{kg}$ and atmospheric pressure is $P_{\mathrm{atm}}=1.01 \times 10^{5} \mathrm{~Pa}$.
(1) How much work is done Piston by this process?
(2) How much heat must be added?
(3) What is the change in the water's internal energy?


## The Mechanical Equivalent of Heat

Joule's original apparatus


## What Happens at the Phase Change? 17



The energy diagram for two atoms.

## Ideal Gases

A weather balloon is loosely inflated to a volume $V_{0}=2.2 \mathrm{~m}^{3}$ with helium at a pressure of $P_{0}=1.0 \times 10^{5} \mathrm{~Pa}$ and a temperature $T_{0}=20^{\circ} \mathrm{C}$. At an elevation of $20,000 \mathrm{ft}$ the atmospheric pressure is down to $P_{1}=0.5 \times 10^{5} \mathrm{~Pa}$ and the temperature is $T_{1}=-48^{\circ} \mathrm{C}$. The bag can expand freely. What is the new volume of the bag? What is the gas mass?


## Ideal Gases

A weather balloon is loosely inflated to a volume $V_{0}=2.2 \mathrm{~m}^{3}$ with helium at a pressure of $P_{0}=1.0 \times 10^{5} \mathrm{~Pa}$ and a temperature $T_{0}=20^{\circ} \mathrm{C}$. At an

| $\underset{\substack{\text { mudpane } \\ \text { ander }}}{\mathbf{H}}$ | 2 |  |  |  |  |  |  | $\substack{\text { Number } \\ \text { Symbol } \\ \text { Name } \\ \text { Atomic Mass }}$ |  |  |  | 13 | 14 | 15 | 16 | 11 | $\stackrel{\substack{\text { Heiln } \\ \text { Hen } \\ 4003}}{ }$ |
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## Absolute Zero and Ideal Gases <br> 20



## Ideal Gases

## 21

A steel tank contains $m_{g}=0.30 \mathrm{~kg}$ of ammonia gas $\left(\mathrm{NH}_{3}\right)$ at an absolute pressure $P_{0}=1.35 \times 10^{5} \mathrm{~N} / \mathrm{m}^{2}$ and a temperature $T_{0}=77^{\circ} \mathrm{C}$. What is the volume of the tank? At a later time the tank is checked. The temperature has fallen to $T_{1}=22^{\circ} \mathrm{C}$ and the pressure has fallen to $P_{1}=8.7 \times 10^{5} \mathrm{~N} / \mathrm{m}^{2}$. How many kilograms of gas leaked out of the tank?


## Boyle's Law for Ideal Gases - 1




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## Boyle's Law for Ideal Gases - 2 <br> 23



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## Specific Heats of Ideal Gases (The Problem) 24

Assume that a pure, ideal gas is made of tiny particles that bounce into each other and the walls of their cubic container of side $\ell$. Show the average pressure $P$ exerted by this gas is

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$$
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$$

Is this right?
$N$ - number of particles $\quad V=\ell^{3}$
$k_{B}$ - Boltzmann constant $m$ - atomic mass
$N_{A}$ - Avogadro's number $\quad v_{\text {total }}$ - atom's speed


## The Kinetic Model of Ideal Gases

(1) The gas consists of a large number of small, mobile particles and their average separation is large.
(2) The particles obey Newton's Laws and the conservation laws, but their motion can be described statistically.
(3) The particles' collisions are elastic on average.
(4) The inter-particle forces are small until they collide.
(6) The gas is pure.
(0) The gas is in thermal equilibrium with the container walls.

## Trajectory of Brownian Motion



## The Plan and the Data



## The Pressure of an Ideal Gas - Impulse and Momentum Change



## The Pressure of an Ideal Gas - Impulse and Momentum Change



## Instantaneous Force 30



## Instantaneous versus Average Force 31



## Instantaneous versus Average Force



## Instantaneous Force in the Gas



## Instantaneous versus Average Force in the Gas 34



## Instantaneous versus Average Force in the Gas 35


(1) Consider a tiny patch of the container.
(2) It's repeatedly hit by gas particles (blue).
(3) The average time separation is $\langle\Delta t\rangle$.

## Instantaneous versus Average Force in the Gas 36


(1) Consider a tiny patch of the container.
(2) It's repeatedly hit by gas particles (blue).
(3) The average time separation is $\langle\Delta t\rangle$.
(4) Average force is red.
(3) Blue area $=$ Red area

## Momentum Conservation and Hitting Walls 37

An atom of mass $m_{h}$ collides elastically head-on with a heavier, stationary, target atom of mass $m_{r}$. Both particles are free to move in space. The initial velocity of the projectile is $\vec{v}_{0}$ as shown below. What is the final velocity $\vec{v}_{1}$ of the projectile in terms of the masses, $\vec{v}_{0}$, and any other constants? What happens to the final velocity $\vec{v}_{1}$ as the target mass $m_{r}$ becomes very large? Ignore the effects of potential energy.

$m_{r}$

## The Plan - Act. 2 of Kinetic Theory of Ideal Gases 38



## Is Potential Energy Important?

A helium atom is moving straight up from the floor of the lab that is at room temperature $T=300 \mathrm{~K}$. Miraculously, the atom never strikes another atom or molecule until it reaches the ceiling at a height $h=4.0 \mathrm{~m}$ above the floor. What is the helium atom's rms speed when it hits the ceiling? How much has its speed changed from the initial speed?

## Specific Heats of Ideal Gases

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C_{V}=\frac{3}{2} N_{A} k_{B}=\frac{3}{2} R
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## The Plan - Activity 2 of Applying the Kinetic Theory42



## The Plan - Activity 3 of Applying the Kinetic Theory43



## The Plan - Activity 4 of Applying the Kinetic Theory44



## The Results

45

$$
\begin{gathered}
P=\frac{1}{3} \frac{N}{V} m \overline{v_{\text {total }}^{2}}=\frac{2}{3} \frac{N}{V}\left\langle E_{\text {kin }}\right\rangle \\
\left\langle E_{\text {kin }}\right\rangle=\frac{3}{2} N k_{B} T \\
C_{V}=\frac{3}{2} N_{A} k_{B}=\frac{3}{2} R
\end{gathered}
$$



## Rotational Kinetic Energy

Classically

$$
K E=\frac{1}{2} m v^{2}=\frac{m^{2} v^{2}}{2 m}=\frac{p^{2}}{2 m}
$$

For rotational motion

$$
E_{\text {rot }}=\frac{L^{2}}{2 \mathcal{I}}
$$

where $L$ is angular momentum and

$$
\mathcal{I}=\sum m r_{i}^{2}=\int r^{2} d m
$$

Quantum mechanically

$$
E_{r o t}^{q m}=\frac{\ell(\ell+1) \hbar^{2}}{2 \mathcal{I}}
$$

where $\ell$ is the angular momentum quantum number.

Hoop or thin cylindrical shell $I_{\mathrm{CM}}=M R^{2}$

Solid cylinder or disk
$I_{\mathrm{CM}}=\frac{1}{2} M R^{2}$

Long, thin rod with rotation axis through center $I_{\mathrm{CM}}=\frac{1}{12} M L^{2}$

Solid sphere
$I_{\mathrm{CM}}=\frac{2}{5} M R^{2}$



Long, thin rod with rotation axis through end $I=\frac{1}{3} M L^{2}$


Thin spherical
shell
$I_{\mathrm{CM}}=\frac{2}{3} M R^{2}$


## A Hint of Quantum Mechanics




## Applying Quantum Mechanics

## 48

How much heat does it take to increase the temperature of $n=4.0$ moles of $\mathrm{H}_{2}$ gas by $\Delta \mathrm{T}=25 \mathrm{~K}$ at room temperature $\mathrm{T}=25^{\circ} \mathrm{C}$ if the gas is held at constant volume? Would the answer change if the gas were $\mathrm{N}_{2}$ ? What about He?

## Calorimetry Measurement



## Thermodynamic Information

TABLE 17.3 Melting/boiling temperatures and heats of transformation

| Substance | $\boldsymbol{T}_{\mathrm{m}}\left({ }^{\circ} \mathbf{C}\right)$ | $\boldsymbol{L}_{\mathrm{f}}(\mathbf{J} / \mathbf{k g})$ | $\boldsymbol{T}_{\mathrm{b}}\left({ }^{\circ} \mathbf{C}\right)$ | $\boldsymbol{L}_{\mathrm{v}}(\mathbf{J} / \mathbf{k g})$ |
| :--- | :---: | :---: | :---: | :---: |
| Nitrogen $\left(\mathrm{N}_{2}\right)$ | -210 | $0.26 \times 10^{5}$ | -196 | $1.99 \times 10^{5}$ |
| Ethyl alcohol | -114 | $1.09 \times 10^{5}$ | 78 | $8.79 \times 10^{5}$ |
| Mercury | -39 | $0.11 \times 10^{5}$ | 357 | $2.96 \times 10^{5}$ |
| Water | 0 | $3.33 \times 10^{5}$ | 100 | $22.6 \times 10^{5}$ |
| Lead | 328 | $0.25 \times 10^{5}$ | 1750 | $8.58 \times 10^{5}$ |

TABLE 17.2 Specific heats and molar specific heats of solids and liquids
Substance $\quad c(\mathrm{~J} / \mathrm{kg} \mathrm{K}) \quad C(\mathrm{~J} / \mathrm{mol} \mathrm{K})$

## Solids

| Aluminum | 900 | 24.3 |
| :--- | :--- | :--- |
| Copper | 385 | 24.4 |

Iron $449 \quad 25.1$

| Gold | 129 | 25.4 |
| :--- | :--- | :--- |

Lead $128 \quad 26.5$

| Ice | 2090 | 37.6 |
| :--- | :--- | :--- |

Liquids

| Ethyl alcohol | 2400 | 110.4 |
| :--- | ---: | ---: |
| Mercury | 140 | 28.1 |
| Water | 4190 | 75.4 |


[^0]:    - $\bigcirc \quad \checkmark \quad$ 位

