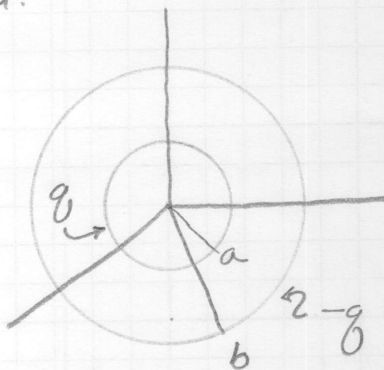


2-34) a.

set $\vec{E}$ firstfor $r < a$

$$\nabla \cdot \vec{E}_1 = \frac{\rho}{\epsilon_0} = 0$$

$$\int \nabla \cdot \vec{E}_1 d\tau = 0$$

$$\oint \vec{E}_1 \cdot d\vec{A} = 0$$

$$\vec{E} = E\hat{r}, d\vec{A} = r^2 d\cos\theta d\phi \hat{r}$$

$$\oint \vec{E}_1 \cdot r^2 d\cos\theta d\phi = 0$$

$$E_1 r^2 \int_0^{2\pi} \int_{-1}^1 d\cos\theta d\phi = 0$$

$$E_1 4\pi r^2 = 0$$

$$\therefore E_1 = 0$$

for $a < r < b$ the left hand side of the previous solution stays the same

$$E_2 4\pi r^2 = \int \frac{\rho}{\epsilon_0} d\tau$$

$$= \frac{1}{\epsilon_0} q$$

$$\therefore E_2 = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$

for $r > b$ the left hand side is the same again

$$E_3 4\pi r^2 = \int \frac{\rho}{\epsilon_0} d\tau$$

$$= \frac{1}{\epsilon_0} (q + (-q))$$

$$= 0$$

$$\therefore E_3 = 0$$

$$W = \frac{\epsilon_0}{2} \int_{\text{all space}} E^2 d\tau \quad d\tau = r^2 dr d\cos\theta d\phi$$

$$= \frac{\epsilon_0}{2} \int_0^{2\pi} \int_0^\pi \int_a^b \left(\frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \right)^2 r^2 dr d\cos\theta d\phi$$

$$= \frac{\epsilon_0}{2} (2)(2\pi) \left(\frac{1}{4\pi\epsilon_0} \right)^2 q^2 \int_a^b \frac{1}{r^2} r^2 dr$$

$$= \frac{1}{2} \left(\frac{1}{4\pi\epsilon_0} \right) q^2 \left(\frac{1}{-1} \right)_a^b$$

$$W = \frac{q^2}{8\pi\epsilon_0} \left(\frac{1}{a} - \frac{1}{b} \right)$$