Can You Improve Upon the GDP Forecasts of Professional Forecasters Using Information About Monetary Policy?

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In this paper, I examine the forecast errors of macroeconomic forecasters to see whether or not their forecasts are efficiently using information about monetary policy. The goal is to investigate, using real-time data, previous research that has found inefficiency in forecasts with respect to monetary policy. I use a real-time data set to investigate the relationship between GDP forecast errors and changes in monetary policy both in-sample and with out-of-sample methods. Out-of-sample results show that exploiting inefficiency is difficult in real time.

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I. Introduction

Do forecasters optimally change their forecasts of GDP growth in response to changes in monetary policy? This question has been answered by a few papers in the literature but mostly using in-sample methods and based on final, revised data. In this paper, I examine the question in a more convincing manner, using real-time data to account more accurately for data revisions, using out-of-sample methods to examine the robustness of in-sample results, and exploring how inefficiency changes over time.

There is a vast literature on the evaluation of forecasts. Point forecasts are evaluated most often using tests of unbiasedness and efficiency. The literature in this area was summed up most clearly by Clark and Mertens (2024), who suggest that forecasts from surveys of professional forecasters are "competitive (albeit not fully optimal) predictors of future outcomes." Recent research has suggested a number of problems with the forecasts of professionals. Bordalo et al. (2020) find that the consensus of forecasts from a survey under-react to news, while individual forecasters over-react, and develop a model of dispersed information to explain it. Clements (2022) shows that individual forecasters are inefficient in their use of information. Bianchi, Ludvigson and Ma (2022) find that individual forecasters suffer from belief distortions but that artificial intelligence algorithms can be used to improve their forecasts. Eva and Winkler (2023), however, find that the research on forecast errors is not very robust and cannot be used to improve on the forecasts in a true real-time out-of-sample experiment. I follow the recent structure of Croushore (2024) to explore whether or not the forecasts can be improved out-of-sample in real-time using end-of-sample or real-time vintage methods (see Koenig, Dolmas and Piger (2003)), accounting for structural instability (see Rossi and Sekhposyan (2010).

The literature suggests that GDP forecasts may not respond appropriately to shocks to monetary policy. Several papers, Ball and Croushore (2003) and Rudebusch and Williams (2009), show that forecasters do not modify their GDP fore-

casts properly when monetary policy changes. I explore the robustness of their results when the analysis includes real-time out-of-sample tests.

II. Data

In this paper, I examine forecasts from the Survey of Professional Forecasters (SPF), which is widely studied.[1] I examine forecasts for real output growth, measured as GNP before 1992 and GDP from 1992 on. The forecasts are made quarterly and the survey asks the respondents to forecast the growth of real output in the current quarter and each of the following four quarters. I examine each of the quarterly annualized forecasts as well as the average output growth forecast over the next four quarters.

Quarterly forecasts for output growth (at an annualized rate) are calculated as in Equation (1):

$$y^f_{t,t+h} = (((\frac{Y^f_{t,t+h}}{Y^f_{t,t+h-1}})^4) - 1) \times 100\%, \tag{1}$$

where $h = 0$, 1, 2, 3, and 4, and $Y^f_{t,t+h}$ is the level of the output forecast made at date t for date $t + h$, using data on output through date $t - 1$.

For testing purposes, I compare those forecasts to realized values, which are calculated as

$$y_{t+h} = ((\frac{Y_{t+h}}{Y_{t+h-1}})^4 - 1) \times 100\%. \tag{2}$$

The forecast error is the realized value of the growth rate minus the forecast

$$e_{t,t+h} = y_{t+h} - y^f_{t,t+h}. \tag{3}$$

[1]The SPF is the only quarterly survey of U.S. macroeconomic forecasters available at no charge, and has been produced on a quarterly basis since 1968. See Croushore and Stark (2019) for a historical discussion of the SPF and the research that uses it. Because of irregularities in the early years of the survey, I start the analysis from the first quarter survey in 1971.

In addition to quarterly forecasts, the SPF can also be used for annual forecasts, both from the current quarter to four-quarters ahead, and from the quarter prior to the forecast date to three-quarters ahead. The average annual output growth rate forecast over quarters t to $t+4$ is calculated in Equation (4):

$$y^{f4}_{t,t+4} = (\frac{Y^{f}_{t,t+4}}{Y^{f}_{t,t}} - 1) \times 100\%. \tag{4}$$

Realized values over the same period are

$$y^{4}_{t+4} = (\frac{Y_{t+4}}{Y_{t}} - 1) \times 100\%. \tag{5}$$

Thus forecast errors for average annual forecasts are equal to

$$e^{4}_{t} = y^{4}_{t+4} - y^{f4}_{t,t+4}. \tag{6}$$

Similarly, I can calculate the average annual forecast growth rate from quarters $t-1$ to $t+3$ by lagging Equation (4) by one quarter; similarly for the realized values and forecast errors.

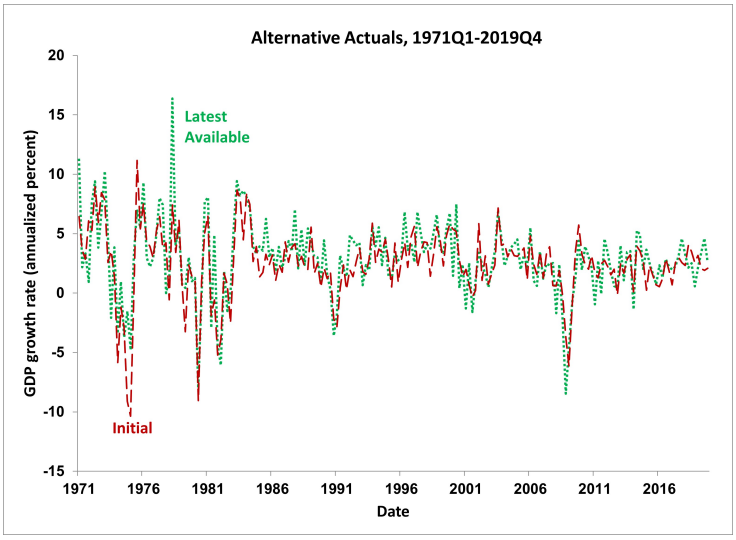
A key question in the forecasting literature is which vintage of the data to use as the realized value in Equations (2) and (5).[2] There are many alternatives and I explore differences across them, comparing initial realized values (the release at the end of the first month of the following quarter), to first final realized values (the release at the end of the third month of the following quarter), to first annual realized values (the release at the end of July of the following year in most years), to pre-benchmark realized values (the last release before a benchmark revision of the National Income and Product Accounts), to latest available realized values (from the latest available vintage of data available when this research started, which was August 2024). I obtain the alternative realized values from the Real-

[2]See Croushore (2011) for a discussion of this issue.

Time Data Set for Macroeconomists (RTDSM), which was created by Croushore and Stark (2001) and made available on the website of the Federal Reserve Bank of Philadelphia. The RTDSM provides information on real output (GNP before 1992, GDP since 1992) and other major macroeconomic variables, as someone standing at the middle of any month from November 1965 to today would have viewed the data. The RTDSM lines up perfectly with the SPF in terms of data availability.

Figure 1 plots GDP growth rates for two of the alternative realized values, initial and latest available, from 1971Q1 to 2019Q4. You can see that the two series generally move together, but there are quarters when they differ substantially, in one case by over ten percentage points. Thus, forecast evaluation conclusions potentially differ significantly depending on the choice of realized values.

Figure 1. Alternative Realized Values

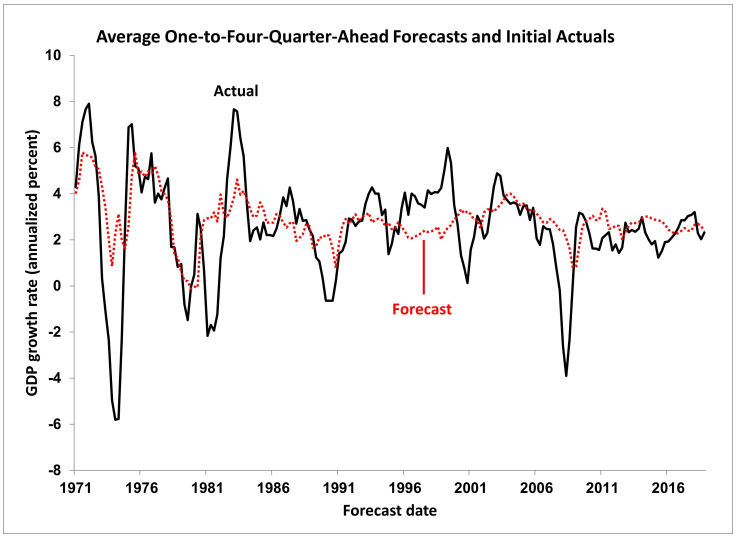


Note: The figure shows the quarterly realized values of GDP growth rates as calculated using Equation (2) based on two alternative concepts: initial and latest available. The graph ends prior to the COVID period, to avoid distortions caused by the large swings to GDP growth in 2020.

To visualize what the realized values and forecasts look like, Figure 2 shows a plot of the forecast for average annual output growth over the next four quarters

(one-to-four-quarters ahead) and the initial realized value of GDP growth over the same horizon. Note that the graph ends prior to the COVID period, to avoid distortions caused by the large swings to GDP growth in 2020; so it uses forecasts from 1971Q1 to 2018Q4, with the corresponding realized values (ending in 2019Q4). As expected, the forecasts are a much smoother series than the object being forecast, and there are some large unanticipated shocks to output.

Figure 2. Average One-to-Four Quarter Ahead Forecasts and Initial Realizations

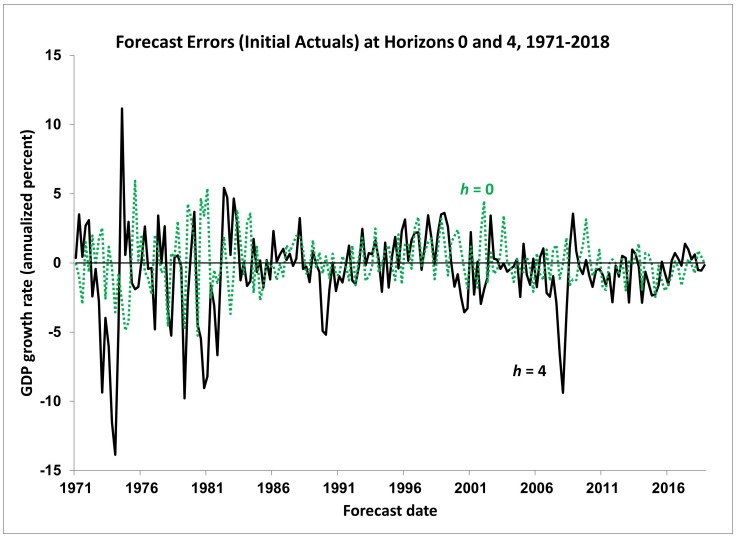


Note: The figure shows the forecast for average annual growth over the next four quarters and the initial realized value of GDP growth over the same horizon. The graph ends prior to the COVID period, to avoid distortions caused by the large swings to GDP growth in 2020; so it uses forecasts from 1971Q1 to 2018Q4, with the corresponding realized values (ending in 2019Q4).

To provide a sense of the size of forecast errors, Figure 3 shows representative forecast errors based on the initial concept of realized values at quarterly horizons 0 and 4. The forecast errors are large and volatile, and they change signs frequently, making them difficult to predict.

To examine whether measures of monetary policy might be used to improve GDP forecasts, I consider three alternative measures of monetary policy: the yield spread, changes in the real federal funds rate, and the Wu-Xia shadow real fed funds rate. For the yield spread, I use the measure of Rudebusch and Williams

FIGURE 3. FORECAST ERRORS AT HORIZONS 0 AND 4



Note: The figure shows the quarterly forecast errors for GDP growth rates as calculated using (3) for two horizons: current quarter ($h = 0$) and four quarters ahead ($h = 4$), and using the initial data release as the realized value. The graph ends prior to the COVID period, to avoid distortions caused by the large swings to GDP growth in 2020; so it uses forecasts from 1971Q1 to 2018Q4, with the corresponding realized values (ending in 2019Q4 at the latest).

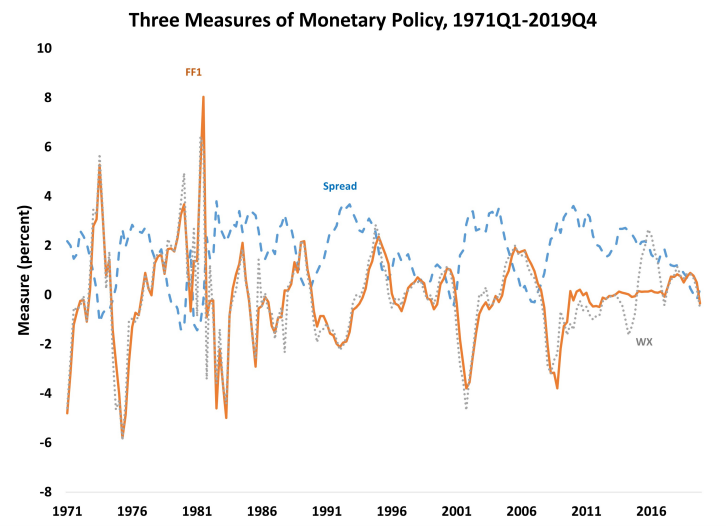
(2009), which is the interest rate on 10-year Treasury notes minus the interest rate on 3-month Treasury bills, using the constant-maturity series for each security. For the change in the real federal funds rate, I use the Ball and Croushore (2003) measure, which is the average federal funds rate in the previous quarter, minus the expected inflation rate over the coming year in the SPF.[3] Note that both the yield spread and the change in the real fed funds rate for the prior quarter are available to the SPF forecasters at the time they make their forecasts. I am careful to only use data available to the forecasters in these efficiency tests. However, in the late 2000s, the nominal federal funds rate became constrained by the effective lower bound on interest rates, so changes in the real federal funds rate may not be as useful as a measure of monetary policy as they were before. To remedy that, I use the shadow real fed funds rate of Wu and Xia (2016), which

[3]Ball and Croushore (2003) examined alternatives to this measure and found that the results were not sensitive to the proxy used.

accounts for nontraditional monetary policy tools and creates an effective federal funds rate based on the impact of those tools.[4] However, the Wu-Xia measure was not available to the forecasters in real time, so our results with this variable are indicative of what a researcher in real time might have found, but are not strictly a real-time result, so are valid only if the revisions to the variable are not large.

The three measures of monetary policy differ somewhat over time but their major movements are correlated, with the real fed funds rate measures having an inverse correlation with the spread measure, as you can see in Figure 4.

FIGURE 4. THREE MEASURES OF MONETARY POLICY



Note: The figure shows the three alternative measures of monetary policy that I use: the term spread between 10-year T-notes and 3-month T-bills (Spread), the change in the real fed funds rate over the previous year ($FF1$), and the change in the Wu-Xia measure of the real fed funds rate over the previous year (WX).

[4]Updated data on the Wu-Xia shadow rate are available online at www.atlantafed.org/cqer/research/wu-xia-shadow-federal-funds-rate.

III. In-Sample Results, Three Approaches

In this section, I investigate whether the three measures of monetary policy are correlated with forecast errors in-sample. The sample uses all SPF forecasts made from 1971Q1 to 2018Q4, so that four-quarter-ahead forecasts end before COVID begins in 2020.

First, I run a regression of each of the forecast errors for the seven horizons and four different measures of realizations for each of the three different measures of monetary policy. The regression is simply:

$$e_{t,t+h} = \alpha + \beta MP_{t-1} + \epsilon_t, \tag{7}$$

where MP_{t-1} is one of the measures of monetary policy through date $t-1$ (known to forecasters making their forecasts at date t) and $e_{t,t+h}$ is a forecast error from Equation (3) or (6). The results are summarized in Table 1.

Table 1—In-Sample Results for Monetary Policy

Horizon	0	1	2	3	4	1-4	0-3
Realized Value							
initial	x x x	x x x	M S M	S S S	S S S	S S S	S S S
first final	x x x	x x x	x M x	x S S	S S S	S S S	S S S
first annual	x x x	x M x	x S M	M S S	S S S	S S S	S S S
pre-benchmark	x x x	x M x	x S M	M S M	S S S	S S S	S S S
latest-available	S S S	x x x	x x x	S x x	S S S	S S x	S M x

Note:

Results of joint test that $\alpha = 0$ and $\beta = 0$: x means p-value > 0.05; M means $0.05 < p$-value < 0.10; S means p-value ≤ 0.05
First term: yield spread; second term: lagged change in real fed funds rate; third term: lagged change in effective (Wu-Xia) real fed funds rate
The sample uses SPF forecasts from 1971Q1 to 2018Q4. Standard errors are adjusted following the Newey and West (1987) procedure.

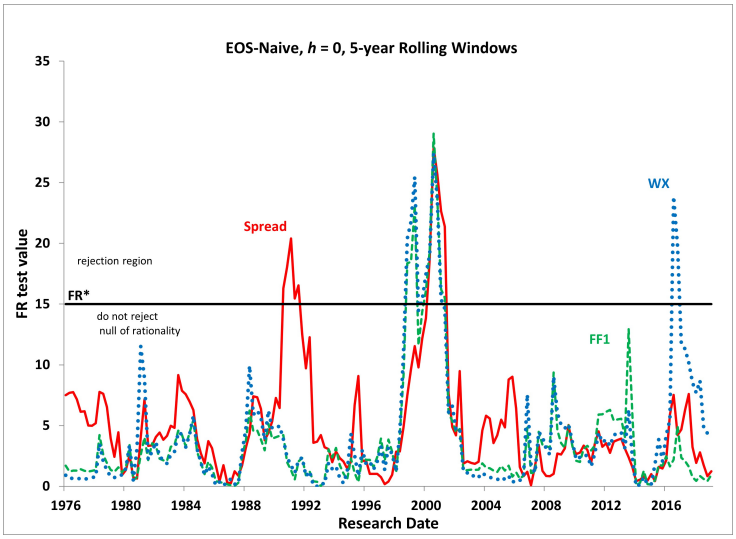
In Table 1, we see that about half of all the cases (denoted "S") show a statistically significant coefficient (p-value ≤ 0.05) in regression Equation (7), which suggests that forecasters are not using information about monetary policy efficiently in forming their forecasts. The coefficients on monetary policy are most often significant at longer horizons, which is consistent with the literature allowing for a lag in the effect of monetary policy on output. In terms of the alternative measures of realized values, the coefficients on monetary policy are more often significant for using first annual or pre-benchmark realized values. Coefficients using the Wu-Xia measure of monetary policy are somewhat less likely to be significant than the other two measures of monetary policy.

These in-sample results, however, are based on the full sample of forecasts made from 1971Q1 to 2018Q4. They do not show how a researcher standing at different points in time would have perceived the inefficiency regressions. Croushore (2024) suggests three methods for viewing inefficiency in real time: End-Of-Sample naive (EOS-naive), End-Of-Sample benchmark-consistent (EOS benchmark-consistent), and Real-Time Vintages (RTV). I consider each of these in turn. For each of these methods, I look at the forecast-rationality statistics of Rossi and Sekhposyan (2016), using 5-year and 10-year rolling windows, with the idea being that even if the full-sample in-sample results do not show inefficiency, that may be because the inefficiencies in short periods offset each other. The method helps identify the periods of inefficiency.

In-Sample Results for EOS-Naive Approach. In the End-Of-Sample-naive approach, we think about a researcher assuming that forecasters at each date use the latest data from FRED or a similar macroeconomic database. The assumption is that the researcher and forecasters ignore any effects of data revisions in evaluating and forming forecasts. So, imagine a researcher standing in 1976Q1, evaluating the current-quarter forecasts from the SPF from 1971Q1 to 1975Q4 (a five-year window), using the latest real GDP growth data from FRED

to analyze the forecasts.[5] Then roll the exercise forward quarter by quarter, maintaining a five-year window each time. Do the same exercise for each of the three different measures of monetary policy and the seven different forecast horizons, allowing for a longer lag in data availability as the horizon lengthens. For each five-year window, calculate the forecast-rationality statistic and compare it with the critical value from Rossi and Sekhposyan (2016). The forecast-rationality statistic is calculated at each research date, and I reject the null hypothesis of forecast rationality if any of the values exceeds the critical value for any research date. The results of this exercise are shown in Figure 5 for the current-quarter horizon. In the discussion that follows, I show results only for the $h = 0$ quarterly horizon and the h =1 to 4 annual horizon, but results for other horizons are also available.

Figure 5. Forecast-Rationality Test Results, EOS-Naive Approach, h = 0, 5-Year Rolling Windows



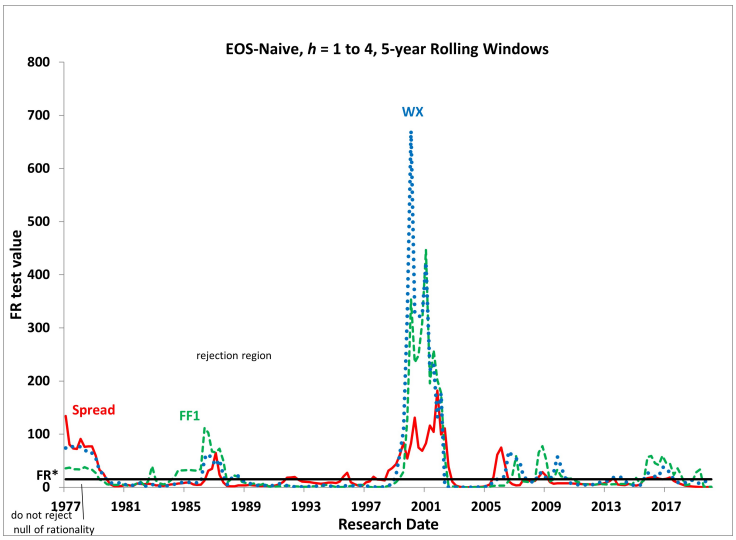
Note: The figure shows the forecast-rationality test results using the EOS-Naive approach with a 5-year rolling window and a horizon of zero. The forecast-rationality critical value is labeled FR*, and I reject forecast rationality if any value across the sample exceeds that threshold. Each line is labeled with the type of monetary policy used in Equation (7), where S is the yield spread, $FF1$ is the lagged change in real fed funds rate, and WX is the lagged change in the effective (Wu-Xia) real fed funds rate.

[5]The research date of 1976Q1 allows for a one-quarter lag for data availability from the last forecast made in 1975Q4.

In Figure 5, we see a few rejections of the null hypothesis of forecast rationality, though not a huge number. We reject forecast rationality based on the yield spread in the early 1990s and based on all three measures in the late 1990s and the early 2000s. For the Wu-Xia measure, there is a rejection in late 2016 to early 2017.

To compare with a longer-horizon forecast, Figure 6 shows the results of the forecast-rationality tests for the 1-to-4 quarter horizon.

FIGURE 6. FORECAST-RATIONALITY TEST RESULTS, EOS-NAIVE APPROACH, H = 1 TO 4, 5-YEAR ROLLING WINDOWS



Note: The figure shows the forecast-rationality test results using the EOS-Naive approach with a 5-year rolling window and a horizon of 1 to 4 quarters. The forecast-rationality critical value is labeled FR*, and we reject forecast rationality if any value across the sample exceeds that threshold. Each line is labeled with the type of monetary policy used in Equation (7), where S is the yield spread, $FF1$ is the lagged change in real fed funds rate, and WX is the lagged change in the effective (Wu-Xia) real fed funds rate.

Figure 6 shows that for this longer horizon, rejections of forecast rationality occur much more frequently than for the current-quarter horizon, and are scattered throughout much of the sample.

Repeating this exercise for 10-year rolling windows leads to qualitatively similar results, though with fewer rejections of forecast rationality than for 5-year

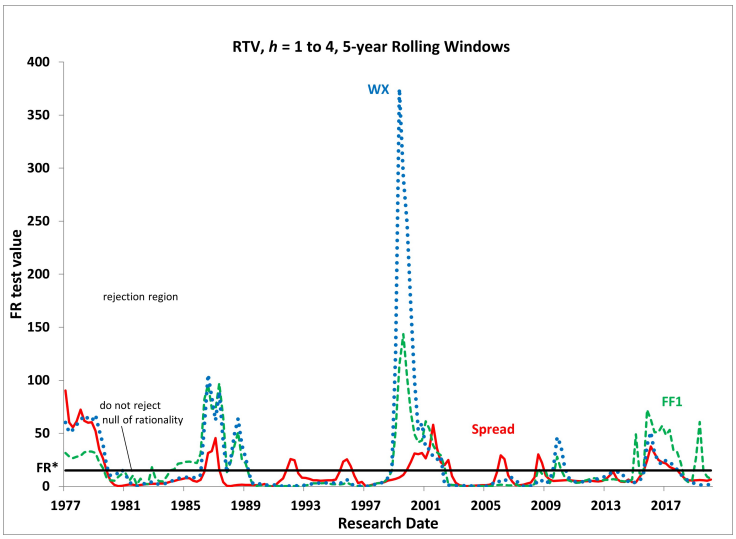
windows, as the figures in the Appendix show. For the current-quarter horizon, rejections occur only around 2000 to 2001 for all three measures of monetary policy. For the 1-to-4 quarter horizon, there are many rejections prior to 1990 but almost none after that. So, clearly rejections of forecast rationality depend on the horizon and the length of the rolling window. There are some differences across measures of monetary policy, as well.

In-sample Results for EOS Benchmark-Consistent Approach. In the End-Of-Sample benchmark-consistent approach, we think about a researcher assuming that forecasters at each date string together pre-benchmark values of the data, with the idea that the DGP differs across benchmark revisions. The assumption is that the researcher and forecasters account for data revisions in evaluating and forming forecasts. The results of the exercises are discussed here; figures showing the results can be found in the Appendix to conserve space.

The forecast-rationality tests for the EOS benchmark-consistent approach show a similar pattern of rejections of forecast rationality as was the case for the EOS-naive approach for 5-year rolling windows with $h = 0$. For the $h = 1$ to 4 horizon, rejections of forecast rationality occur much more frequently than for $h = 0$ and are scattered throughout much of the sample, similar to the EOS-naive results. Results for the EOS benchmark-consistent approach in 10-year rolling windows are also similar to the EOS-naive approach.

In-sample Results for RTV Approach. In the real-time-vintage approach, we think about a researcher assuming that forecasters at each date look at data vintages with similar ages, with the idea that the DGP differs across concepts of realized values. In particular, especially for forecasting initial values, using just the initial release values in the forecasting model might be appropriate. The assumption is that the researcher and forecasters view the DGP as relating initial releases to each other over time. Results for the RTV approach differ somewhat from the EOS approaches, so I show the results here for the $h = 1$ to 4 horizon, with other results in the Appendix.

FIGURE 7. FORECAST-RATIONALITY TEST RESULTS, RTV APPROACH, H = 1 TO 4, 5-YEAR ROLLING WINDOWS



Note: The figure shows the forecast-rationality test results using the RTV approach with a 5-year rolling window and a horizon of 1 to 4 quarters. The forecast-rationality critical value is labeled FR*, and we reject forecast rationality if any value across the sample exceeds that threshold. Each line is labeled with the type of monetary policy used in Equation (7), where S is the yield spread, $FF1$ is the lagged change in real fed funds rate, and WX is the lagged change in the effective (Wu-Xia) real fed funds rate.

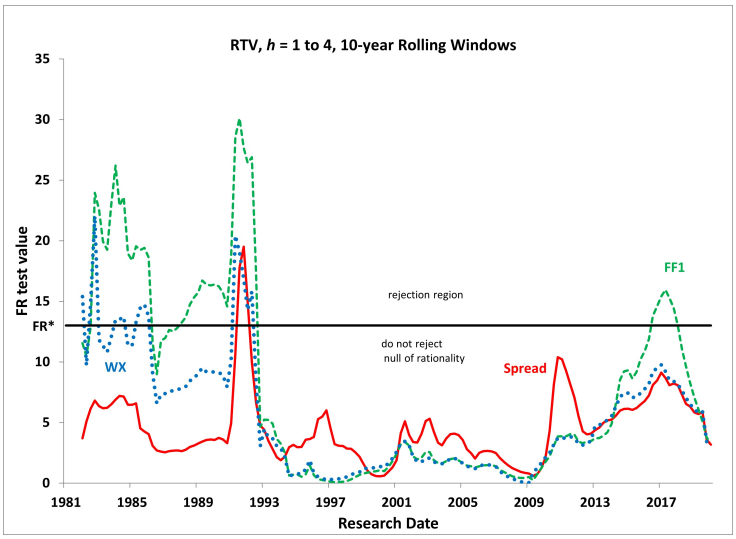
Figure 7 shows that for this longer horizon with the RTV approach, there are many rejections of forecast rationality. There are many more rejections than for the $h = 0$ horizon, and also many more than for the EOS approaches.

Repeating this exercise for 10-year rolling windows leads to many fewer rejections of forecast rationality than for 5-year windows, as Figure 8 shows.

IV. Forecast-Improvement Exercises for Inefficiency in Real Time

Given the in-sample results, I proceed to investigate the possibility of using the regression results from Equation (7) to improve upon the SPF forecasts in a simulated real-time out-of-sample exercise; I call this a forecast-improvement exercise (FIE). Taking the estimated $\hat{\alpha}$ and $\hat{\beta}$, and recalling from Equation (3) that $e_{t,t+h} = y_{t+h} - y^f_{t,t+h}$, I create, at each date t, an improved forecast $y^i_{t,t+h}$, where

FIGURE 8. FORECAST-RATIONALITY TEST RESULTS, RTV APPROACH, H = 1 TO 4, 10-YEAR ROLLING WINDOWS



Note: The figure shows the forecast-rationality test results using the RTV approach with a 10-year rolling window and a horizon of 1 to 4 quarters. The forecast-rationality critical value is labeled FR*, and we reject forecast rationality if any value across the sample exceeds that threshold. Each line is labeled with the type of monetary policy used in Equation (7), where S is the yield spread, $FF1$ is the lagged change in real fed funds rate, and WX is the lagged change in the effective (Wu-Xia) real fed funds rate.

$$y^i_{t,t+h} = y^f_{t,t+h} + (\delta_{1,t} \times \hat{\alpha}) + (\delta_{2,t} \times \hat{\beta} MP_{t-1}), \tag{8}$$

where the δ terms will be described below. The baseline case has both δ terms equal to 1.

Using Equations (7) and (8), I simulate the activity of a real-time forecaster, forming improved forecasts at each date based only on the real-time data and past forecast errors available at each date.[6] I collect all the improved forecasts over that period and calculate root-mean-squared-forecast errors ($RMSFE$s) for each different horizon and each different measure of monetary

[6]In the out-of-sample exercise, I use only data that the forecasters would have known in real time when the SPF survey results are released, using the data only up to the quarter prior to the SPF forecast. (The exception is for the Wu-Xia shadow rate because real-time data for it do not exist.) The coefficients of the regression are re-estimated at each date.

policy. I compare those $RMSFE$s to those of the SPF forecast, dividing the $RMSFE$ of the attempt to improve on the survey by the $RMSFE$ of the SPF, to generate a relative $RMSFE$ ($RRMSFE$). An $RRMSFE$ greater than one means the attempt to improve on the SPF forecasts actually made them worse, while an $RRMSFE$ less than one means the attempt to improve on the SPF succeeded.[7]

I consider four different versions of Equation (8). The baseline case has $\delta_{1,t} = 1$ and $\delta_{2,t} = 1$ for all t. This method does not account for estimation error in the coefficients, however. To account for estimation error, I could shrink the estimated coefficients towards zero. As a simple first pass, I shrink the coefficients by half, so that $\delta_{1,t} = 0.5$ and $\delta_{2,t} = 0.5$ for all t. (I leave it for future research to determine optimal shrinkage in these forecast-improvement exercises.) An alternative is to use the information from the forecast-rationality tests to allow the δ terms to vary over time. One possibility is to set the δ terms to zero, if the FR-test value is less than the critical value at that date, or equal to one, if the FR-test value is greater than the critical value at that date. Another possibility is to use shrinkage with that method. So, I try all four adjustment methods to see how the results vary.

There are many results of these forecast-improvement exercises: 2 rolling window sizes (5 year and 10 year), 3 approaches (EOSn, EOSbc, RTV), 3 measures of monetary policy (S, $FF1$, WX), 7 horizons (0, 1, 2, 3, 4, 1 to 4, 0 to 3), and 4 adjustment methods (full, full with shrinkage, FR-test based, FR-test based with shrinkage), for a total of 504 sets of results.

In what follows, I first focus on the 1-to-4 quarter-ahead horizon, with other results shown later. Table 2 shows the results for the EOS-naive approach for the 1-to-4 quarter horizon. In only 2 of the 24 cases is the $RRMSFE$ equal to 1 (if carried out to additional decimal points, one of them is 1.0001, the other is 0.9996); all the rest show that the attempt to improve the forecasts actually

[7]Statistical significance of differences between the surveys is tested using the Harvey, Leybourne and Newbold (1997) modified Diebold and Mariano (1995) test statistic of the corresponding null hypothesis.

makes them worse, with 1 of them statistically significantly worse (at the 5 percent level).

TABLE 2—*RRMSFEs* AND *P*-VALUES FOR FORECAST IMPROVEMENT EXERCISES, EOS-NAIVE APPROACH WITH REALIZED VALUES = INITIAL, $h = 1$ TO 4

Monetary Policy Measure	S		$FF1$		WX	
Window Size: Adjustment Method	5-yr	10-yr	5-yr	10-yr	5-yr	10-yr
All	1.330	1.097	1.324	1.051	1.421	1.047
	[0.01]	[0.09]	[0.15]	[0.21]	[0.20]	[0.24]
All, shrink	1.089	1.018	1.085	1.004	1.118	1.003
	[0.08]	[0.51]	[0.26]	[0.84]	[0.26]	[0.87]
$FR > cv$	1.215	1.008	1.288	1.010	1.370	1.001
	[0.10]	[0.47]	[0.20]	[0.71]	[0.25]	[0.81]
$FR > cv$, shrink	1.061	1.002	1.085	1.000	1.103	1.000
	[0.20]	[0.61]	[0.24]	[0.99]	[0.30]	[0.89]

Note: The table shows relative-root-mean-squared errors ($RRMSFE$) and p-values of the Diebold-Mariano test [in square brackets] for forecasts in forecast-improvement exercises, using the EOS-naive approach with realized values = initial. The sample consists of one-year-ahead SPF forecasts made from 1971Q1 to 2018Q4.

I can follow the same procedure for the EOS benchmark-consistent approach, as shown in Table 3, with results that are not too different from the EOS-naive approach. Two of the cases show statistically significantly worse forecasts, 20 others show worse forecasts that are not statistically significant, and 2 show improved forecasts, though not statistically significantly so.

I follow the same procedure using the RTV approach. For the 1-to-4 horizon, the results in Table 4 show 4 cases of significantly worse forecasts, while 2 show minor forecast improvement that is not statistically significant.

To summarize the results for the 1-to-4-quarter horizon, Tables 2 to 4 show that the attempt to improve on the SPF forecasts is successful in fewer than

TABLE 3—*RRMSFEs* AND *P*-VALUES FOR FORECAST IMPROVEMENT EXERCISES, EOS BENCHMARK-CONSISTENT APPROACH WITH REALIZED VALUES = INITIAL, $h = 1$ TO 4

Monetary Policy Measure	S		$FF1$		WX	
Window Size: Adjustment Method	5-yr	10-yr	5-yr	10-yr	5-yr	10-yr
All	1.450	1.117	1.375	1.062	1.512	1.077
	[0.02]	[0.11]	[0.15]	[0.31]	[0.17]	[0.15]
All, shrink	1.124	1.022	1.088	1.002	1.143	1.013
	[0.06]	[0.54]	[0.33]	[0.96]	[0.24]	[0.65]
$FR > cv$	1.345	1.018	1.339	1.034	1.448	0.997
	[0.04]	[0.31]	[0.19]	[0.41]	[0.22]	[0.83]
$FR > cv$, shrink	1.101	1.006	1.093	1.004	1.125	0.994
	[0.09]	[0.31]	[0.28]	[0.83]	[0.29]	[0.48]

Note: The table shows relative-root-mean-squared errors ($RRMSFE$) and p-values of the Diebold-Mariano test [in square brackets] for forecasts in forecast-improvement exercises, using the EOS benchmark-consistent approach with realized values = initial. The sample consists of one-year-ahead SPF forecasts made from 1971Q1 to 2018Q4.

TABLE 4—*RRMSFEs* AND *P*-VALUES FOR FORECAST IMPROVEMENT EXERCISES, RTV APPROACH WITH REALIZED VALUES = INITIAL, $h = 1 - 4$

Monetary Policy Measure	S		$FF1$		WX	
Window Size: Adjustment Method	5-yr	10-yr	5-yr	10-yr	5-yr	10-yr
All	1.327	1.072	1.293	1.035	1.361	1.033
	[0.02]	[0.08]	[0.18]	[0.30]	[0.20]	[0.25]
All, shrink	1.100	1.020	1.072	1.003	1.094	1.004
	[0.03]	[0.33]	[0.31]	[0.87]	[0.29]	[0.82]
$FR > cv$	1.216	1.002	1.277	1.016	1.335	0.996
	[0.04]	[0.32]	[0.19]	[0.32]	[0.22]	[0.69]
$FR > cv$, shrink	1.069	1.001	1.078	1.001	1.091	0.995
	[0.05]	[0.32]	[0.25]	[0.90]	[0.28]	[0.37]

Note: The table shows relative-root-mean-squared errors ($RRMSFE$) and p-values of the Diebold-Mariano test [in square brackets] for forecasts in forecast-improvement exercises, using the EOS benchmark-consistent approach with realized values = initial. The sample consists of one-year-ahead SPF forecasts made from 1971Q1 to 2018Q4.

10 percent of the cases, and the improvement is never statistically significant. Improvement is more likely using the results of the forecast-rationality test as a guide to when to adjust the forecasts. For most cases, the attempt to improve on the SPF forecasts makes the forecasts worse, with about 10 percent of the cases in which the improved forecasts are statistically significantly worse than the original SPF forecasts.

Looking more generally across all the horizons, and not just at the 1-to-4 quarter horizon, in what follows I show summary tables of the results, followed by some general description of which procedures are most likely to lead to better adjustments to the SPF forecasts.

I begin with an overall summary table, with the results of all 504 permutations of 2 rolling window sizes, 3 approaches, 3 measures of monetary policy, 7 horizons, and 4 adjustment methods. Table 5 shows the results.

Table 5—Forecast Improvement Exercises Counts of Ranges, All Permutations

$RRMSFE$ range	$RRMSFE$s in range	p-value ≤ 0.05
1.10 to ∞	100	35
1.02 to 1.10	180	17
1.00 to 1.02	194	2
0.98 to 1.00	30	0
0.90 to 0.98	0	0
0.00 to 0.90	0	0

Note: The table shows the numbers of cases in which the relative-root-mean-squared error ($RRMSFE$) falls within the given range, and the number of cases with p-values of the Diebold-Mariano test that are less than or equal to 0.05, across all 504 permutations of 2 rolling window sizes, 3 approaches, 3 measures of monetary policy, 7 horizons, and 4 adjustment methods. The sample consists of SPF forecasts made from 1971Q1 to 2018Q4.

As Table 5 shows, there are no statistically significant improvements to the forecasts. In no cases out of 504 is there more than 2 percent improvement in the $RMSFE$. In about 6 percent of the cases, there is a small improvement on the SPF forecasts of less than 2 percent of the SPF $RMSFE$, and the improvement

is never statistically significant. In the other 474 cases out of 504, which is 94 percent of all cases, the attempt to improve the forecasts makes them worse; they are statistically significantly worse in about 11 percent of all the cases. In about 20 percent of the cases, the attempt to improve on the forecasts made the $RMSFE$ rise by more than 10 percent.

In the next set of tables, I generalize the results across different permutations, such as across horizons, approaches, rolling-window sizes, measures of monetary policy, and adjustment methods.

Table 6 shows the results across five quarterly horizons. Looking across the horizons, it appears most likely to find improved forecasts at the current-quarter horizon of $h = 0$. The most statistically significant cases of making the forecasts worse are for $h = 2$. Horizons $h = 1$ and $h = 4$ show the least likelihood of forecast improvement.

Table 6—Forecast Improvement Exercises Counts of Ranges, Across Quarterly Horizons

$RRMSFE$	$h=0$		$h=1$		$h=2$		$h=3$		$h=4$	
range	N	p	N	p	N	p	N	p	N	p
1.10 to ∞	3	3	9	4	14	10	13	3	13	2
1.02 to 1.10	19	2	30	4	29	0	25	0	28	8
1.00 to 1.02	39	0	33	0	23	0	28	0	30	1
0.98 to 1.00	11	0	0	0	6	0	6	0	1	0
0.90 to 0.98	0	0	0	0	0	0	0	0	0	0
0.00 to 0.90	0	0	0	0	0	0	0	0	0	0

Note: The table shows the numbers of cases in which the relative-root-mean-squared error ($RRMSFE$) falls within the given range, and the number of cases with p-values of the Diebold-Mariano test that are less than or equal to 0.05, across all 72 permutations of 2 rolling window sizes, 3 approaches, 3 measures of monetary policy, and 4 adjustment methods for each of the 5 quarterly forecast horizons. The sample consists of SPF forecasts made from 1971Q1 to 2018Q4.

Table 7 shows the two annual horizons. Looking across the horizons, it appears more likely to find improved forecasts at the annual horizon of $h = 1$ to 4, rather than $h = 0$ to 3. Similarly, there are more cases of statistically significantly worse forecasts for the $h = 0$ to 3 horizon than for $h = 1$ to 4.

Table 7—Forecast Improvement Exercises Counts of Ranges, Across Annual Horizons

$RRMSFE$ range	h=1 to 4 N	p	h=0 to 3 N	p
1.10 to ∞	25	5	23	8
1.02 to 1.10	22	2	27	1
1.00 to 1.02	20	0	21	1
0.98 to 1.00	5	0	1	0
0.90 to 0.98	0	0	0	0
0.00 to 0.90	0	0	0	0

Note: The table shows the numbers of cases in which the relative-root-mean-squared error ($RRMSFE$) falls within the given range, and the number of cases with p-values of the Diebold-Mariano test that are less than or equal to 0.05, across all 72 permutations of 2 rolling window sizes, 3 approaches, 3 measures of monetary policy, and 4 adjustment methods for each of the 2 annual forecast horizons. The sample consists of SPF forecasts made from 1971Q1 to 2018Q4.

Table 8 shows results across the three different approaches (EOS-naive, EOS benchmark-consistent, and RTV). Looking across the approaches, it appears most likely to find improved forecasts using the RTV approach, and less likely with the EOSn approach. The most significant forecast worsening is for EOSn.

Table 9 shows the two different windows, 5-year and 10-year. Looking across the window sizes, it appears more likely to find improved forecasts using 10-year windows, and to find more forecasts with $RMSFEs$ that are worse by 10 percent or more using 5-year windows. Using 5-year windows leads to many more significant forecast worsenings than 10-year windows.

Table 10 shows results across the three different measures of monetary policy (S, $FF1$, and WX). Looking across the measures, it appears most likely to find improved forecasts using the $FF1$ measure, and least likely with the spread measure. Using the spread measure is most likely to make the forecasts worse, often significantly so.

Table 11 shows the four different types of adjustments. Looking across the adjustment methods, it appears most likely to find improved forecasts using shrinkage. Full adjustment without shrinkage is particularly poor, and leads to statis-

Table 8—Forecast Improvement Exercises Counts of Ranges, Across Approaches

$RRMSFE$	EOSn		EOSbc		RTV	
range	N	p	N	p	N	p
1.10 to ∞	31	14	44	14	25	7
1.02 to 1.10	65	7	59	5	56	5
1.00 to 1.02	66	0	55	0	73	2
0.98 to 1.00	6	0	10	0	14	0
0.90 to 0.98	0	0	0	0	0	0
0.00 to 0.90	0	0	0	0	0	0

Note: The table shows the numbers of cases in which the relative-root-mean-squared error ($RRMSFE$) falls within the given range, and the number of cases with p-values of the Diebold-Mariano test that are less than or equal to 0.05, across all 168 permutations of 2 rolling window sizes, 3 measures of monetary policy, 7 horizons, and 4 adjustment methods for each of the 3 approaches. The sample consists of SPF forecasts made from 1971Q1 to 2018Q4.

Table 9—Forecast Improvement Exercises Counts of Ranges, Across Window Sizes

$RRMSFE$	5-year		10-year	
range	N	p	N	p
1.10 to ∞	98	35	2	0
1.02 to 1.10	115	5	65	12
1.00 to 1.02	32	0	162	2
0.98 to 1.00	7	0	23	0
0.90 to 0.98	0	0	0	0
0.00 to 0.90	0	0	0	0

Note: The table shows the numbers of cases in which the relative-root-mean-squared error ($RRMSFE$) falls within the given range, and the number of cases with p-values of the Diebold-Mariano test that are less than or equal to 0.05, across all 252 permutations of 7 horizons, 3 approaches, 3 measures of monetary policy, and 4 adjustment methods for each of the 2 window sizes: 5-year and 10-year. The sample consists of SPF forecasts made from 1971Q1 to 2018Q4.

Table 10—Forecast Improvement Exercises Counts of Ranges, Across Measures of Monetary Policy

$RRMSFE$	S		$FF1$		WX	
range	N	p	N	p	N	p
1.10 to ∞	32	23	28	8	40	4
1.02 to 1.10	63	9	62	3	55	5
1.00 to 1.02	70	0	68	2	56	0
0.98 to 1.00	3	0	10	0	17	0
0.90 to 0.98	0	0	0	0	0	0
0.00 to 0.90	0	0	0	0	0	0

Note: The table shows the numbers of cases in which the relative-root-mean-squared error ($RRMSFE$) falls within the given range, and the number of cases with p-values of the Diebold-Mariano test that are less than or equal to 0.05, across all 168 permutations of 2 rolling window sizes, 3 approaches, 7 horizons, and 4 adjustment methods for each of the 3 measures of monetary policy. The sample consists of SPF forecasts made from 1971Q1 to 2018Q4.

tically significant worsening of forecasts in 43 out of 126 cases.

V. Summary and Conclusions

To summarize the results of this myriad of tests, I have shown that inefficiency holds in-sample, based on standard tests on the forecast errors. However, the attempt to improve on the SPF forecasts out of sample is generally not successful and sometimes makes the forecasts significantly worse. I accounted carefully for different approaches to thinking about the data-generating process, data revisions, and structural instability. The most promising avenues for forecast improvement seem to be using the RTV approach, the $FF1$ measure of monetary policy, a 10-year window size, adjusting using the FR test with shrinkage, and using the current-quarter forecast or the annual forecast at the horizon from 1 to 4 quarters ahead.

Why might in-sample results show a relationship between macroeconomic variables and forecast errors, but out-of-sample results do not? It may be that forecasters do not recognize the importance of a variable for forecasting until some

Table 11—Forecast Improvement Exercises Counts of Ranges, Across Adjustment Methods

$RRMSFE$	Full		Full shrink		$FR > cv$		$FR > cv$ shrink	
range	N	p	N	p	N	p	N	p
1.10 to ∞	56	27	8	1	32	7	4	0
1.02 to 1.10	60	15	60	1	24	0	36	1
1.00 to 1.02	9	1	48	0	65	1	72	0
0.98 to 1.00	1	0	10	0	5	0	14	0
0.90 to 0.98	0	0	0	0	0	0	0	0
0.00 to 0.90	0	0	0	0	0	0	0	0

Note: The table shows the numbers of cases in which the relative-root-mean-squared error ($RRMSFE$) falls within the given range, and the number of cases with p-values of the Diebold-Mariano test that are less than or equal to 0.05, across all 72 permutations of 2 rolling window sizes, 3 approaches, 3 measures of monetary policy, and 7 horizons, for each of the 4 adjustment methods. The sample consists of SPF forecasts made from 1971Q1 to 2018Q4.

time passes, so there is an in-sample relationship that is not useful for forecasting for very long. Or it may take forecasters some time to adjust to structural shifts as they learn about the long run, as discussed by Farmer, Nakamura and Steinsson (2024). Or, as Cukierman, Lustenberger and Meltzer (2020) suggest, a permanent-transitory confusion may lead to in-sample correlations, even if forecasters have rational expectations.

The structure of the forecast-improvement exercises in this paper is based on the in-sample results reported by others in the literature, cited in the Introduction. Some possible future extensions of this work include testing additional variables that might affect real GDP growth forecasts and modifying the degree of shrinkage or looking for optimal shrinkage.

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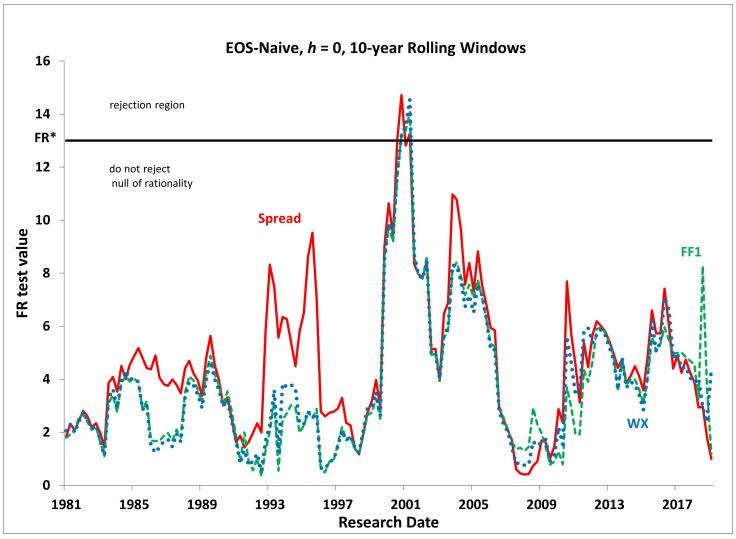
VI. Appendix

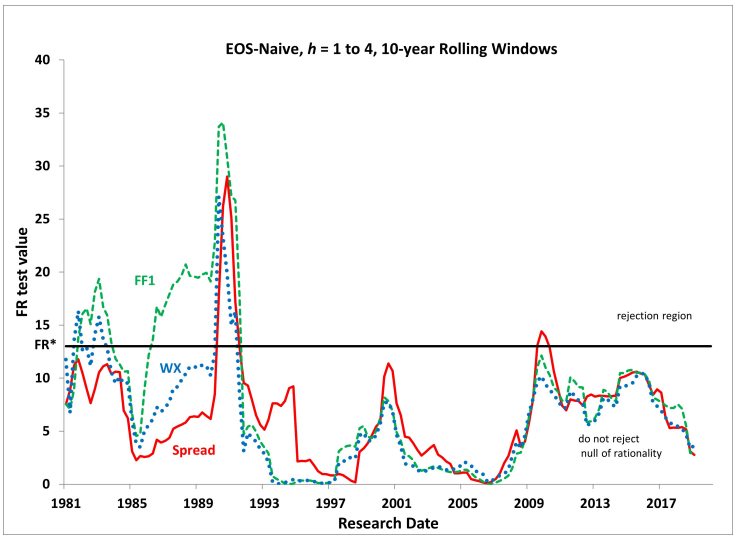
This Appendix shows many of the graphs and tables discussed in the main body of the paper that were removed from the body of the paper to make it more succinct.

Figure 9. Forecast-Rationality Test Results, EOS-Naive Approach, h = 0, 10-Year Rolling Windows



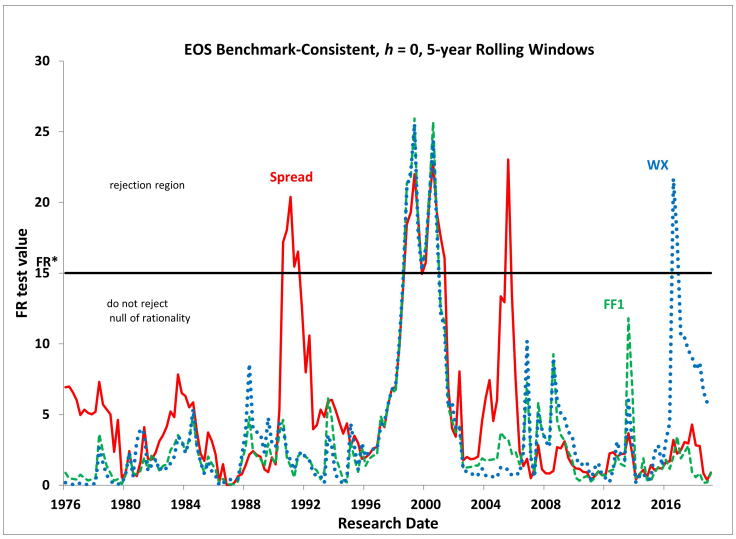
Note: The figure shows the forecast-rationality test results using the EOS-Naive approach with a 10-year rolling window and a horizon of zero. The forecast-rationality critical value is labeled FR*, and we reject forecast rationality if any value across the sample exceeds that threshold. Each line is labeled with the type of monetary policy used in Equation (7).

FIGURE 10. FORECAST-RATIONALITY TEST RESULTS, EOS-NAIVE APPROACH, H = 1 TO 4, 10-YEAR ROLLING WINDOWS



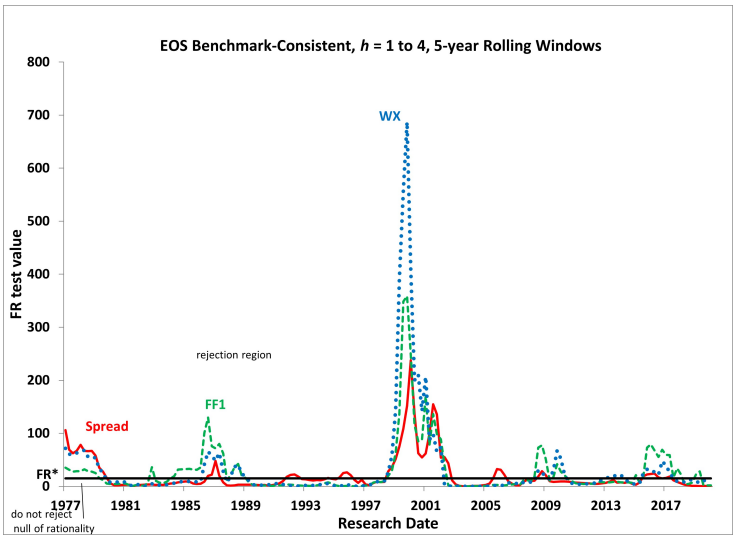
Note: The figure shows the forecast-rationality test results using the EOS-Naive approach with a 10-year rolling window and a horizon of 1 to 4 quarters. The forecast-rationality critical value is labeled FR*, and we reject forecast rationality if any value across the sample exceeds that threshold. Each line is labeled with the type of monetary policy used in Equation (7).

FIGURE 11. FORECAST-RATIONALITY TEST RESULTS, EOS BENCHMARK-CONSISTENT APPROACH, H = 0, 5-YEAR ROLLING WINDOWS



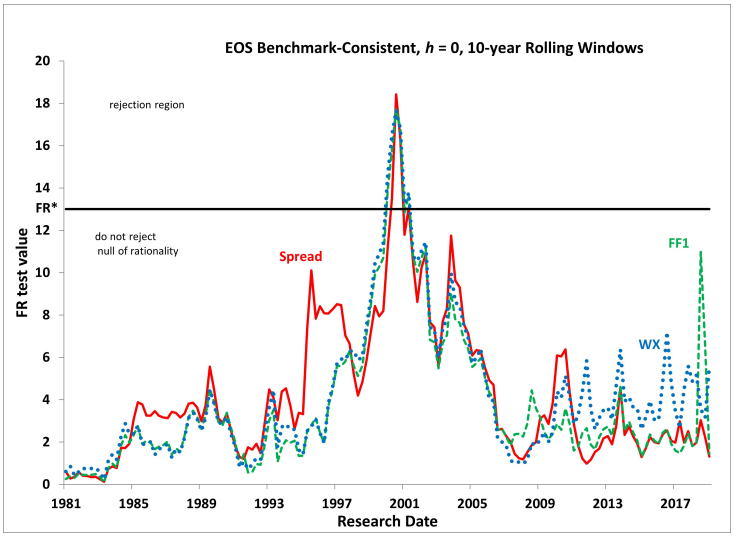
Note: The figure shows the forecast-rationality test results using the EOS Benchmark-Consistent approach with a 5-year rolling window and a horizon of zero. The forecast-rationality critical value is labeled FR*, and we reject forecast rationality if any value across the sample exceeds that threshold. Each line is labeled with the type of monetary policy used in Equation (7).

FIGURE 12. FORECAST-RATIONALITY TEST RESULTS, EOS BENCHMARK-CONSISTENT APPROACH, H = 1 TO 4, 5-YEAR ROLLING WINDOWS



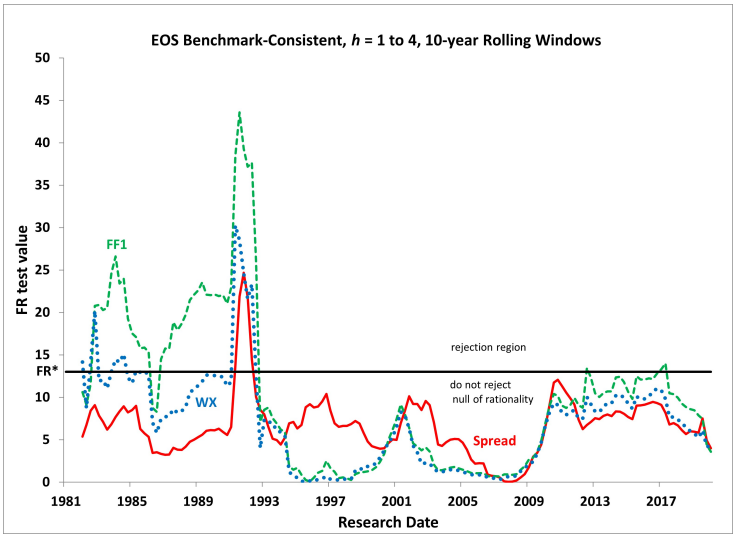
Note: The figure shows the forecast-rationality test results using the EOS Benchmark-Consistent approach with a 5-year rolling window and a horizon of 1 to 4 quarters. The forecast-rationality critical value is labeled FR*, and we reject forecast rationality if any value across the sample exceeds that threshold. Each line is labeled with the type of monetary policy used in Equation (7).

FIGURE 13. FORECAST-RATIONALITY TEST RESULTS, EOS BENCHMARK-CONSISTENT APPROACH, H = 0, 10-YEAR ROLLING WINDOWS



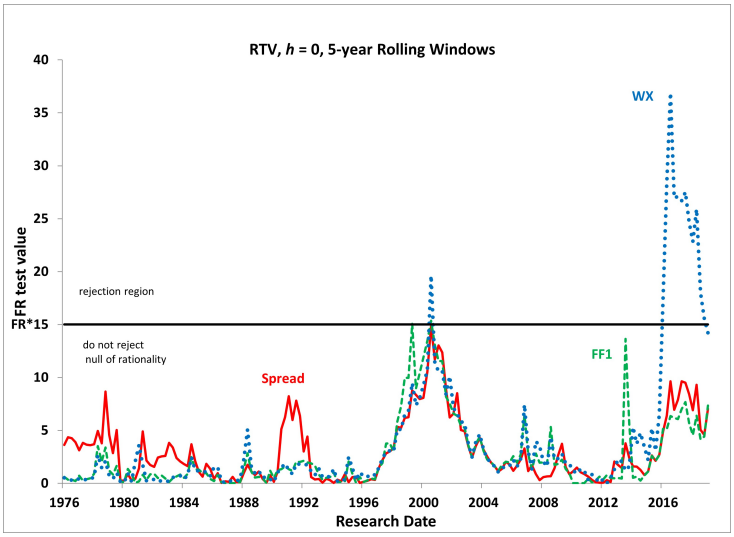
Note: The figure shows the forecast-rationality test results using the EOS Benchmark-Consistent approach with a 10-year rolling window and a horizon of zero. The forecast-rationality critical value is labeled FR*, and we reject forecast rationality if any value across the sample exceeds that threshold. Each line is labeled with the type of monetary policy used in Equation (7).

FIGURE 14. FORECAST-RATIONALITY TEST RESULTS, EOS BENCHMARK-CONSISTENT APPROACH, H = 1 TO 4, 10-YEAR ROLLING WINDOWS



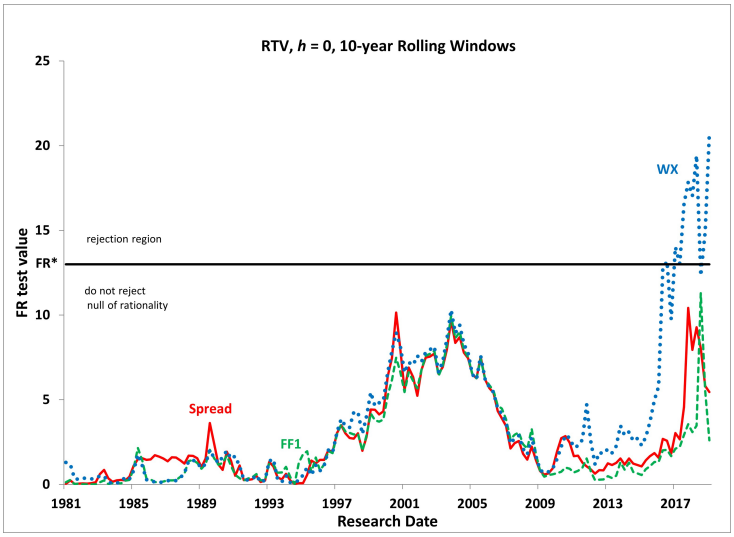
Note: The figure shows the forecast-rationality test results using the EOS Benchmark-Consistent approach with a 10-year rolling window and a horizon of 1 to 4 quarters. The forecast-rationality critical value is labeled FR*, and we reject forecast rationality if any value across the sample exceeds that threshold. Each line is labeled with the type of monetary policy used in Equation (7).

FIGURE 15. FORECAST-RATIONALITY TEST RESULTS, RTV APPROACH, H = 0, 5-YEAR ROLLING WINDOWS



Note: The figure shows the forecast-rationality test results using the RTV approach with a 5-year rolling window and a horizon of zero. The forecast-rationality critical value is labeled FR*, and we reject forecast rationality if any value across the sample exceeds that threshold. Each line is labeled with the type of monetary policy used in Equation (7).

FIGURE 16. FORECAST-RATIONALITY TEST RESULTS, RTV APPROACH, H = 0, 10-YEAR ROLLING WINDOWS



Note: The figure shows the forecast-rationality test results using the RTV approach with a 10-year rolling window and a horizon of zero. The forecast-rationality critical value is labeled FR*, and we reject forecast rationality if any value across the sample exceeds that threshold. Each line is labeled with the type of monetary policy used in Equation (7).