#### Why Does Saturn Have Rings?

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The rings of Saturn were discovered by Galileo in 1610, but its rings were not understood until the work of Christiaan Huygens in 1659. The photograph is a composite of 165 images taken by the Cassini spacecraft over nearly three hours on September 15, 2006. UV, IR, and clear-filter images were used and the colors adjusted to resemble natural color.



More information is here. Are there any other important objects in the image?

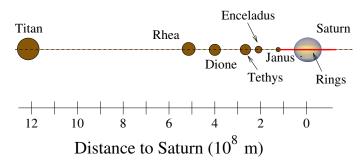
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The figure shows the position of Saturn's rings and the orbital radii of some of Saturn's satellites. The sizes of Saturn and the satellites are not to scale, but the distances from the center of Saturn are to scale. Roche's limit is a calculation performed in the mid-nineteenth century by a French physicist Edward Roche to explain the structure of Saturn's rings and moons. Is Roche's limit correct? More here.

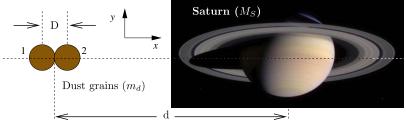
# **Saturn's Rings and Moons**



Titan's shadow can be seen on the image of Saturn (from the Hubble Space Telescope).

Two, identical, spherical dust grains of mass  $m_d$  are orbiting Saturn in a circle just touching one another and aligned along a radius from the planet's center (see figure).

- ① What is the time difference between their periods T after one orbit if  $d = 10^8 \ m$  and  $D = 10^{-3} \ m$ ?
- ② What is the difference  $\Delta \vec{F} = \vec{F}_2 \vec{F}_1$  between the forces due to the gravity of Saturn on each dust grain in terms of the constants in the figure and any others?
- **3** Show that if  $d \gg D$  then  $|\Delta \vec{F}| = 2GM_s m_d D/d^3$ .
- **①** Compare  $\Delta \vec{F}$  with the gravitational attraction between the two dust grains  $F_{21}$ . When will the grains stick together? For what values of d?
- Since we don't know the size of the grains (D) recast the problem in terms of the the density  $\rho = 2 \times 10^3 \ kg/m^3$  of the dust. What is Roche's limit?

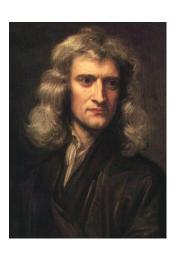


- Consider a body with no net force acting on it. If it is at rest it will remain at rest. If it is moving with a constant velocity it will continue to move at that velocity.
- For all the different forces acting on a body

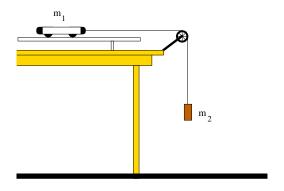
$$\Sigma \vec{F_i} = m\vec{a}$$
 .

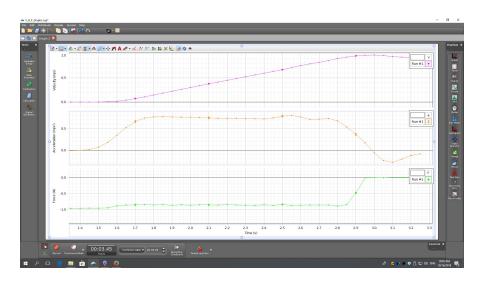
Solution For every action there is an equal and opposite reaction.

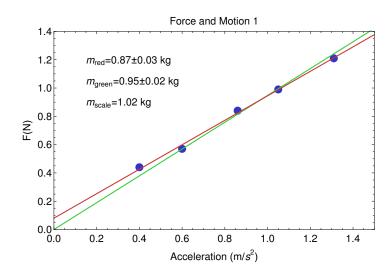
$$\vec{F}_{AB} = -\vec{F}_{BA}$$

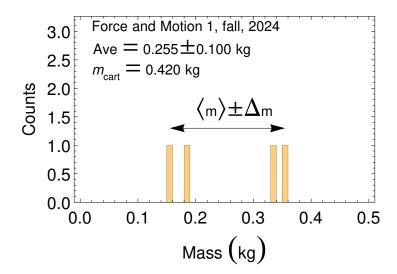


Two blocks are connected by a rope draped over a pulley as shown below. The masses are  $m_1 = 1.0 \ kg$  and  $m_2 = 4.0 \ kg$ . What is the acceleration of both masses?

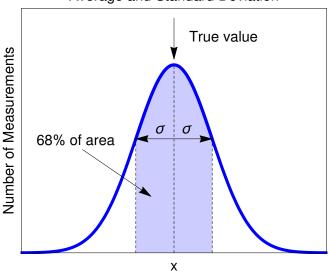












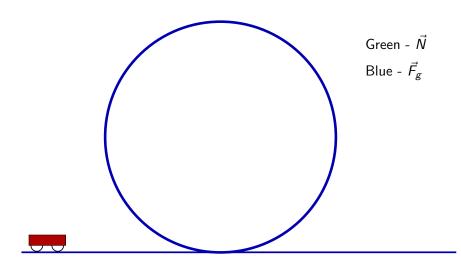
You are an engineer who has to hang a kinetic sculpture (a mobile) by the famed artist Alexander Calder from the crossbeams of the hall of an art gallery. Consider the two cables used to hold up the mobile of mass m=210~kg from a ceiling as shown below. They are attached at two seperate points on the ceiling as shown where  $\theta_1=28^\circ$  and  $\theta_2=47^\circ$  to the horizontal. What is the tension in each cable?

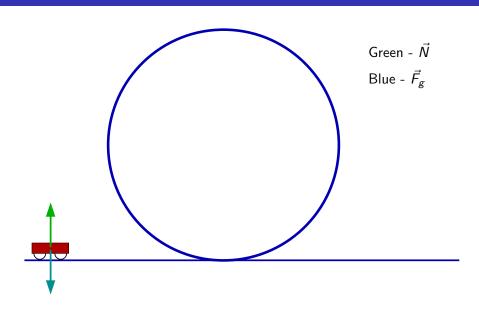
ALEXANDER CALDER (American, 1898-1976) The Star, 1960 Polychrome sheet metal and steel wire 35-3/4 × 53-3/4 × 17-5/8"

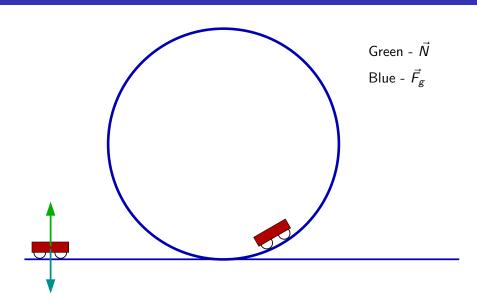


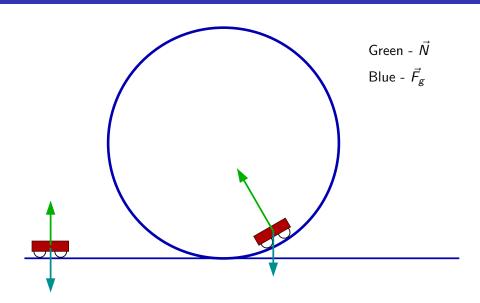
The Anaconda is a popular roller coaster roller coaster at the King's Dominion amusement part north of Richmond. It contains the loop in it's track shown below. If the radius of the loop is  $R=6.3\ m$ , then what is the minimum speed at the top of the loop that is necessary to prevent someone from falling out?

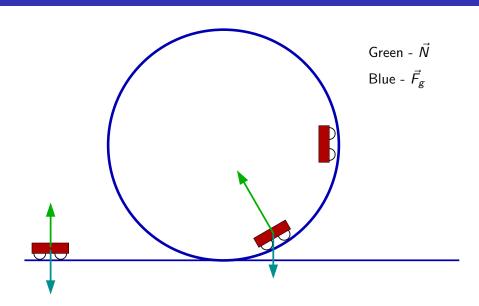


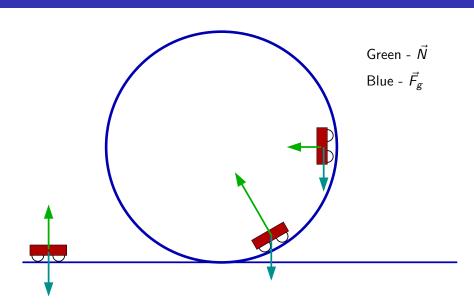


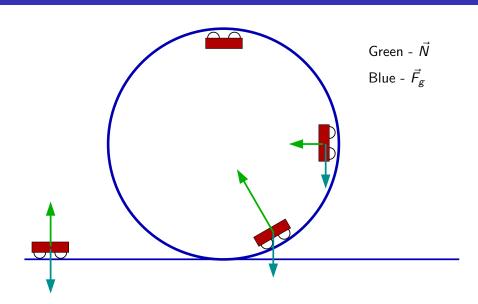


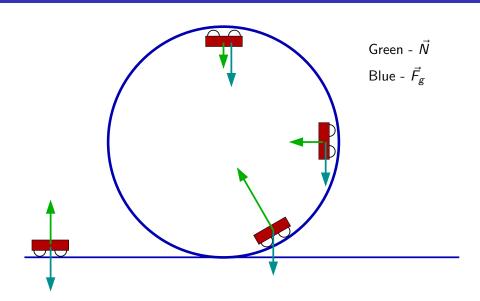


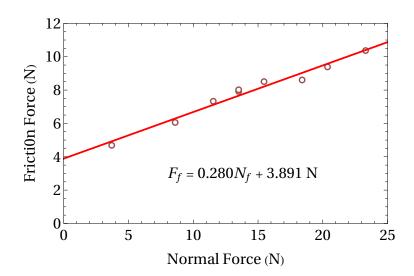












The Rotor is an amusement park ride in which a room shaped like a cylinder is spun rapidly forcing the occupants to lean against the wall. When a minimum rotational frequency is reached the floor of the room is suddenly dropped. Of course, the riders remain safely pinned to the walls

of the spinning room. What is the minimum rotational frequency for this ride to work properly? The radius of the room is r=2.1~m and the coefficient of friction between the walls and the backs of the riders is  $\mu=0.4$ .

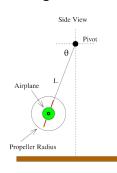


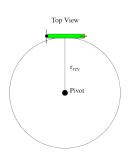
Materials	$\mu_{s}$	$\mu_k$
Steel on steel	0.74	0.57
Aluminum on steel	0.61	0.47
Copper on steel	0.53	0.36
Rubber on concrete	1.0	0.8
Wood on wood	0.25-0.5	0.2
Glass on glass	0.94	0.4
Waxed wood on wet snow	0.14	0.1
Waxed wood on dry snow	_	0.04
Ice on ice	0.1	0.03
Teflon on Teflon	0.04	0.04
Human synovial joints	0.01	0.003

Consider the model airplane hanging from a string and flying in a circle as shown in the figure. Some of the parameters of the plane's orbit are shown below. What is the tension in the string?

#### Some useful information

 $\begin{array}{ll} \text{Mass } (m) & 0.17 \ \textit{kg} \\ \text{String length}(\textit{L}) & 0.7 \ \textit{m} \\ \text{Orbital Period}(\textit{t}_{rev}) & 1.61 \ \textit{s} \\ \text{Orbital Radius}(\textit{r}_{rev}) & 0.295 \ \textit{m} \end{array}$ 











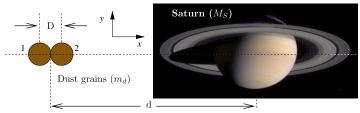


by xkcd

Force	Relative	Range of Force	Mediating	Mass of Field Par-
	Strength		Field Particle	ticle ( ${ m GeV/c^2}$ )
Nuclear	1	Short, 1 fm	Gluon	0
Electromagnetic	$10^{-2}$	$\infty$	Photon	0
Weak	$10^{-5}$	Short, $10^{-5}~\mathrm{fm}$	$W^{\pm}, Z^{0}$	80.4, 80.4, 91.2
Gravitational	$10^{-41}$	$\infty$	Graviton	0

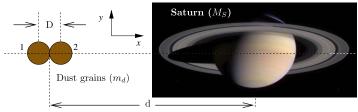
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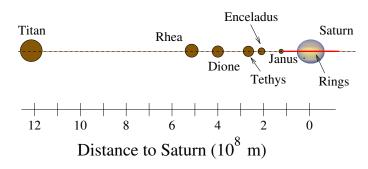
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- What is the and D = 1 How do we test this?  $| t | | d = 10^8 \text{ m}$
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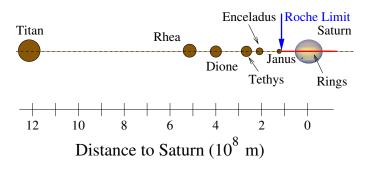
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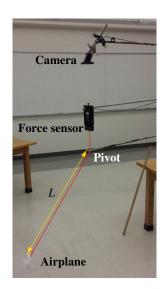


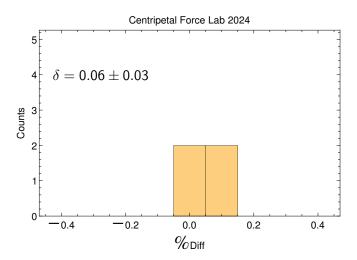
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Planet	Roche Limit (m)	Distance to Nearest Satellite (m)
Earth	$2.3 \times 10^7$	$38 \times 10^7$
Mars	$1.1 \times 10^7$	$0.94 \times 10^{7}$
Jupiter	$1.5  imes 10^8$	$1.3  imes 10^8$
Saturn	$1.1 \times 10^8$	$1.4  imes 10^8$
Uranus	$5.5 \times 10^7$	$5.0  imes 10^7$
Neptune	$5.8 \times 10^7$	$3.6  imes 10^7$
Pluto	$3.0  imes 10^6$	$48  imes 10^6$

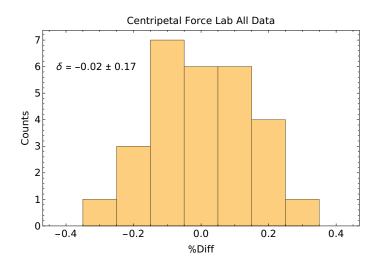
### Hints for the Centripetal Force lab

- Activities 1-4 have already been done in Lab 8. Copy them over.
- Align the camera, string, and the plane in the center of the field of view. Make sure the camera is pointing straight down.
- Use the ruler to calibrate.
- Use the distance from the hole in the post to the center of the airplane. It should not exceed about 45 cm.
- Set the airplane run for about five or so orbits to let any oscillations die out.
- **1** Weigh the plane on the scale when you're done.
- ② Go to Create → Measuring Tools → Tape Measure in Tracker to measure the diameter of the plane's trajectory in several places on a Tracker frame showing all your steps. If there is a large variation in your measurement consult your instructor.

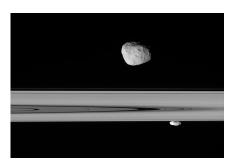




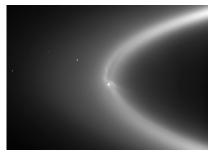
## Results for the Centripetal Force lab (All Data) 33



#### Some cool pictures



From just beneath the ringplane, Cassini stares at Janus (181 kilometers across) on the near side of the rings and Prometheus (102 kilometers across) on the far side.



A cryovolcanic eruption on Enceladus, a moon of Saturn, can be seen in this Cassini image along with the diffuse ring produced by these eruptions.