

A Star Is Born!

The photograph below shows a cloud of molecules called Bernard 68 (B68). It is located about 300 light-years $(2.8 \times 10^{15} \text{ km})$ away from us in the constellation Ophiuchus and is about 1.6 trillion kilometers across. It is made of molecules like CS, N_2H , H_2 , and CO and is slowly rotating ($\omega = 9.4 \times 10^{-14}$ rad/s). The internal gravitational attraction of B68 may make the molecular cloud collapse far enough so it will ignite the nuclear fires and B68 will begin to shine.

A Star Is Born 4

The molecular cloud B68 in the constellation Ophiuchus is rotating with an angular speed $\omega = 9.4 \times 10^{-14}$ rad/s. The gravitational attraction among the atoms in the cloud may make it collapse until the core is hot enough to ignite nuclear reactions and B68 will begin to shine. If the final properties of B68 are the same as our Sun, i.e., the same mass and size, then what will be its final angular velocity and period? Assume the lost mass carries away very little angular momentum. Compare this with the angular velocity of the Sun. Is your result reasonable? Why or why not?

 $M_{B68} = 6.04 \times 10^{30}$ kg $I_{B68} = 2.7 \times 10^{54}$ kg – km² $M_{Sun} = 1.989 \times 10^{30}$ kg $R_{Sun} = 6.96 \times 10^5$ km $T_{Sun} = 25.4$ d

Rotational Quantities 5

Linear \rightarrow Rotational Quantities 6

$$
\vec{r}_{cm} = \frac{\sum m_i \vec{r}_i}{\sum m_i}
$$

The pulsar in the Crab nebula has a period $T_0 = 0.033$ s and this period has been observed to be increasing by $\Delta\,{\cal T}=1.26\times 10^{-5}$ s each year. Assuming constant angular acceleration what is the expression for the angular displacement of the pulsar? What are the values of the parameters in that expression?

$$
m_C = 3.4 \times 10^{30} \text{ kg}
$$

$$
r_C = 25 \times 10^3 \text{ m}
$$

A Pulsar 8

Linear \rightarrow Rotational Quantities 9

$$
\vec{r}_{cm} = \frac{\sum m_i \vec{r}_i}{\sum m_i}
$$

$\vec{F} \propto \vec{a} \rightarrow \vec{F} = m\vec{a}$ 10

Force and Motion 1

Torque - Rotational Equivalent of Force 11

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Consider a point particle at a fixed distance from the origin (attached by the famed massless rod or a string) that moves in a circle.

 \vec{r}

Consider a point particle at a fixed distance from the origin (attached by the famed massless rod or a string) that moves in a circle.

$$
\vec{F} = m\vec{a} \rightarrow \vec{\tau} = r\vec{F}_{\perp} = (mr^2) \alpha
$$

 \vec{r}

origin

Jerry Gilfoyle [A Star Is Born!](#page-0-0) 10 / 38 Jerry Gilfoyle A Star Is Born!

Torque - Rotating a Rigid Body (a door) 14

Torque - Rotating a Rigid Body (a door) 15

Moments of Inertia **16**

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Linear \rightarrow Rotational Quantities 17

$$
\vec{r}_{cm} = \frac{\sum m_i \vec{r}_i}{\sum m_i}
$$

The shield door at a neutron test facility at Lawrence Livermore Laboratory is possibly the world's heaviest hinged door. It has a mass $m =$ 44, 000 kg , a rotational inertia about a vertical axis through its hinges of $I=8.7\times10^4$ kg m^2 , and a (front) face width of $w = 2.4$ m. A steady force $\vec{F_a}=73$ N , applied at its outer edge and perpendicular to the plane of the door, can move it from rest through an angle $\theta = 90^{\circ}$ in $\Delta t =$ 75 s. What is the torque exerted by the friction in the hinges?

Moments of Inertia **19**

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Rotational Form of $\vec{F} = m\vec{a}$ in lab 20

A wooden disk and a metal ring have the same mass m and radius r , start from rest, and roll down identical inclined planes (see figure). Which one wins?

Which One Wins? 22

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Rolling Down an Incline - 1 24

Link to video is [here.](https://facultystaff.richmond.edu/~ggilfoyl/genphys/131/20181103_140133.mp4) Link to Tracker project file is [here.](https://facultystaff.richmond.edu/~ggilfoyl/genphys/131/rolling2018b.trz)

Rolling Down an Incline - 4 27

More [here](https://facultystaff.richmond.edu/~ggilfoyl/genphys/131/examples/flyingRacket.pdf) (pdf) and [here](https://facultystaff.richmond.edu/~ggilfoyl/genphys/131/examples/youtubeCM1.trz) (trz).

A wooden disk and a metal ring have the same mass m and radius r , start from rest, and roll down identical inclined planes (see figure). Which one wins?

Linear \rightarrow Rotational Quantities 29

$$
\vec{r}_{cm} = \frac{\sum m_i \vec{r}_i}{\sum m_i}
$$

Moments of Inertia **30**

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A Star Is Born 31

The molecular cloud B68 in the constellation Ophiuchus is rotating with an angular speed $\omega = 9.4 \times 10^{-14}$ rad/s. The gravitational attraction among the atoms in the cloud may make it collapse until the core is hot enough to ignite nuclear reactions and B68 will begin to shine. If the final properties of B68 are the same as our Sun, i.e., the same mass and size, then what will be its final angular velocity and period? Assume the lost mass carries away very little angular momentum. Compare this with the angular velocity of the Sun. Is your result reasonable? Why or why not?

$$
M_{B68} = 6.04 \times 10^{30} \text{ kg} \qquad I_{B68} = 2.7 \times 10^{54} \text{ kg} - \text{km}^2 \qquad M_{Sun} = 1.989 \times 10^{30} \text{ kg}
$$

$$
R_{Sun} = 6.96 \times 10^5 \text{ km} \qquad T_{Sun} = 25.4 \text{ d}
$$

The Shape It's In 32

The plot below shows the 'obscuration' in the angular area around B68 based on measurements of background stars. The light in the center is 10^{14} dimmer than outside the edge of the cloud. To make life simple we will treat the mass distribution of B68 as three, rigid, uniform spheres that lie along the axis shown in the figure and rotate with $\omega = 9.4 \times 10^{-14}$ rad/s. The spheres do NOT rotate independently of the rest of the cloud. The origin is at the center of the central lobe. What is the moment of inertia of the cloud?

ESO PR Photo 29c/99 (2 July 1999)

Angular Momentum 33

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Angular Momentum 34

$$
0.2006\text{ Brooks} \text{Cole} \cdot \text{Therefore}
$$

$$
|\vec{L}| = r p_{\perp} = l \omega
$$

 \sum

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Conservation of Momentum From $\vec{F}_{BA}=-\vec{F}_{AB}-36$

$$
\vec{F}_{AB} = -\vec{F}_{BA} \qquad \frac{d\vec{p}_A}{dt} = -\frac{d\vec{p}_B}{dt}
$$
\n
$$
m_A \vec{a}_A = -m_B \vec{a}_B \qquad \frac{d\vec{p}_A}{dt} + \frac{d\vec{p}_B}{dt} = 0
$$
\n
$$
m_A \frac{d\vec{v}_A}{dt} = -m_B \frac{d\vec{v}_B}{dt} \qquad \frac{d}{dt} (\vec{p}_A + \vec{p}_B) = 0
$$
\n
$$
\frac{dm_A \vec{v}_A}{dt} = -\frac{dm_B \vec{v}_B}{dt} \qquad \therefore \ \vec{p}_A + \vec{p}_B = const
$$

Torque and Rotational Energy - An Application 37

A trebuchet is a device used in the Middle Ages to throw big rocks at castles and is now used to throw other things like pumpkins, [pianos,](http://www.youtube.com/watch?v=hZxCEkGk6HI) Consider the figures below. The trebuchet has a stiff wooden beam of mass $m_b = 15$ kg and length $l_b = 5$ m with masses $m_c = 700$ kg (the counterweight) and $m_p = 0.1$ kg (the payload) on it's ends. Treat these two masses as point particles. A frictionless axle is located a distance $d = 0.15$ m from the counterweight. The beam is released from rest in a horizontal position. We will launch the payload from a bucket at the end of the beam . What is the maximum speed the payload can reach before it leaves the bucket?

Angular Momentum Conservation 38

Angular Momentum Conservation 39

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Angular Momentum Conservation 41

 \overline{a} the company and more card $70 - 10$ **Co Bi** Page #1 nak. π **ØTRF&`ØZ`AXY⊹KA#`⋌**|XX|☆■XQ|≠◎● Period of Botation 36 \overline{m} T Run #2 angular velocity \mathbf{r} Period of Rotation Dun #2 $\overline{}$ 75 **Secondary Secondary** $\overline{1}$ nisa 14 $\overline{2}$ 0.54 $\overline{3}$ 0.55 13 $\overline{4}$ 0.55 s 0.55 12 $\begin{picture}(20,20) \put(0,0){\dashbox{0.5}(10,0){ }} \put(10,0){\dashbox{0.5}(10,0){ }} \put(10,0){\dashbox{$ $\overline{6}$ 0.56 $\overline{11}$ $\overline{1}$ 0.56 \overline{a} 0.56 10 $\overline{9}$ 0.57 $\overline{10}$ 0.57 Ž ϵ $\overline{\mathbf{H}}$ 0.58 $\overline{12}$ 0.58 × 16.601 s, 5.91 rad/s Ġ. $\overline{13}$ 0.58 j 14 0.59 $\overline{15}$ 0.59 $\overline{16}$ 0.59 p $\overline{17}$ 0.60 18 0.60 × 19 0.61 $\overline{20}$ 0.99 \overline{a} 21 1.05 \overline{a} $\overline{22}$ 1.08 23 1.09 $\overline{2}$ 24 1.11 25 1.12 ï 26 1.14 ż. ø 10 12 14 16 18 20 $\overline{22}$ 24 26 27 1.15 Time (s) 28 Angular Velocity vs. Time Controls 3 $\begin{array}{|c|c|c|c|c|}\hline \textbf{0.124.30} & \textbf{0.124.30} & \textbf{Comman Rate = -Hz} \\ \hline \textbf{0.124.30} & \textbf{0.124.30} & \textbf{0.124.30} & \textbf{0.124.30} \\ \hline \end{array}$ $\begin{array}{|c|c|c|c|c|}\hline \textbf{10} & \textbf{0} & \textbf{0} & \textbf{-1} \\ \hline \textbf{2122} & \textbf{222} & \textbf{0} & \textbf{0} & \textbf{0} & \textbf{0} \\ \hline \end{array}$ \mathcal{P} . Type here to search **B q** ■ ● B D 中 00 ENG

A Star Is Born 42

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Newton's 2nd Law for Rotation 43

